

Clustering and SRC

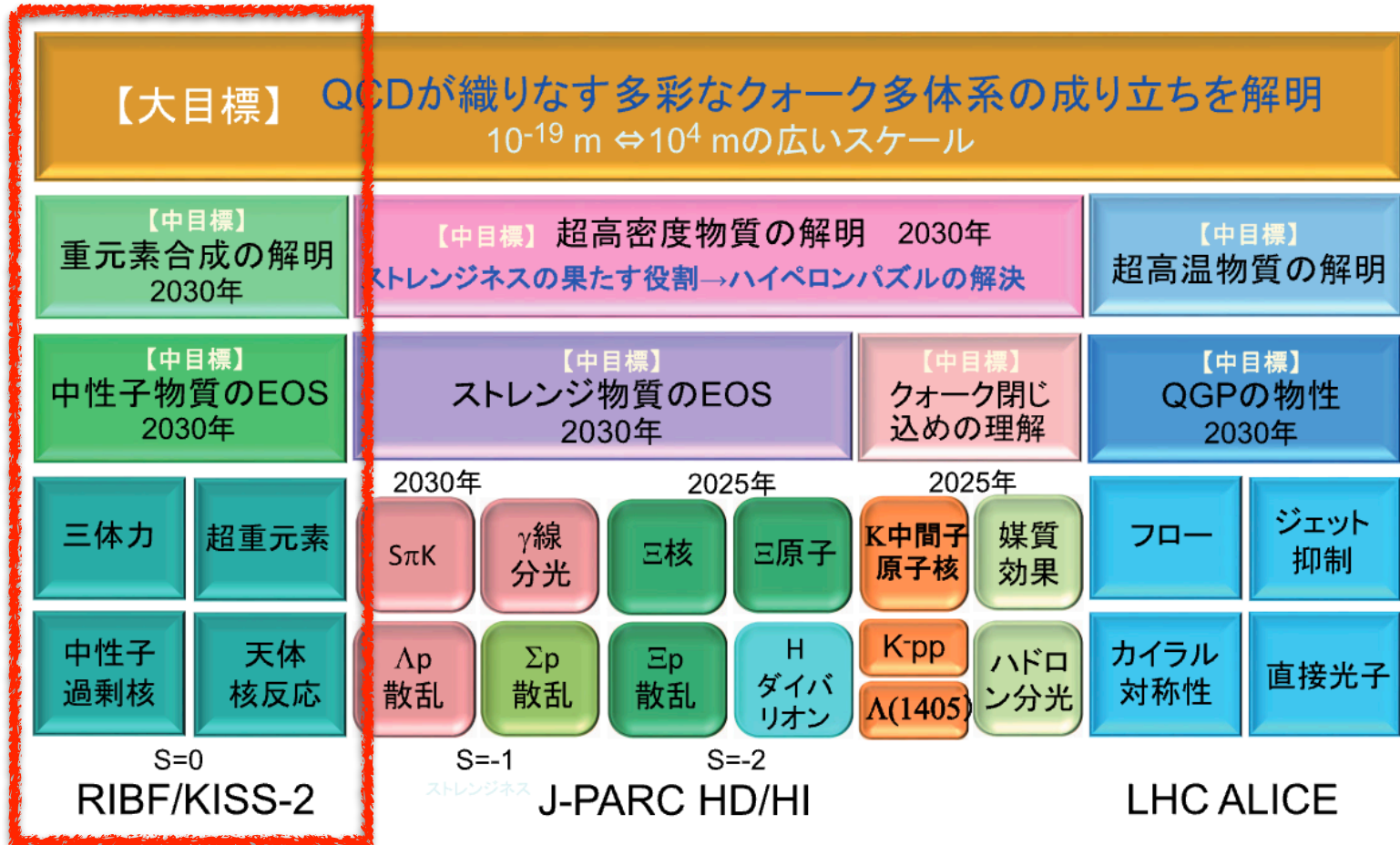
Recent topics from low energy nuclear physics

Yuki Kubota

RIKEN Nishina Center

Low energy nuclear physics

日本の核物理の将来レポート (2021年版)



Low energy nuclear physics

日本の核物理の将来レポート (2021年版)

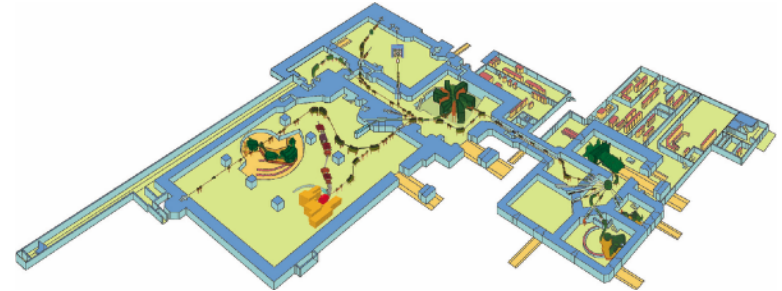


RCNP, Osaka

p : 392 MeV

Double-arm spectrometer

Grand-Raiden & LAS



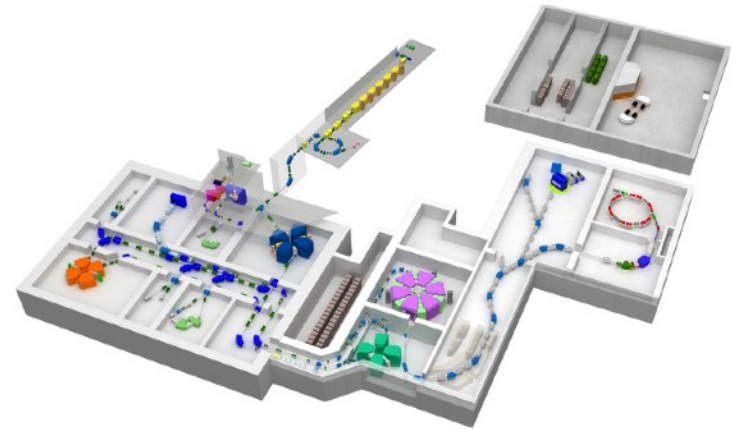
RIBF, RIKEN

^{238}U : 345 MeV/u

→ RI beam

3 spectrometers

- SAMURAI
- ZeroDegree
- SHARAK/OEDO



Low energy nuclear physics

日本の核物理の将来レポート (2021年版)



Lifecycle

Program Advisory Committee (PAC) meeting

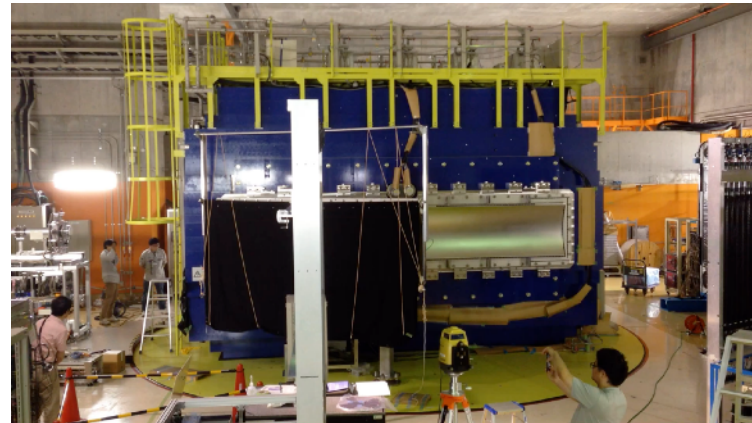
Once or twice per year

Approved → expired in 4 years

Experiment

Beam time: ~ a week

Setup: scrap and build



Low energy nuclear physics

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Lifecycle

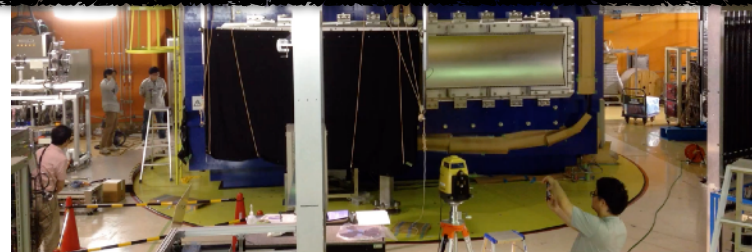
Pro

Variety of topics/programs in this field.

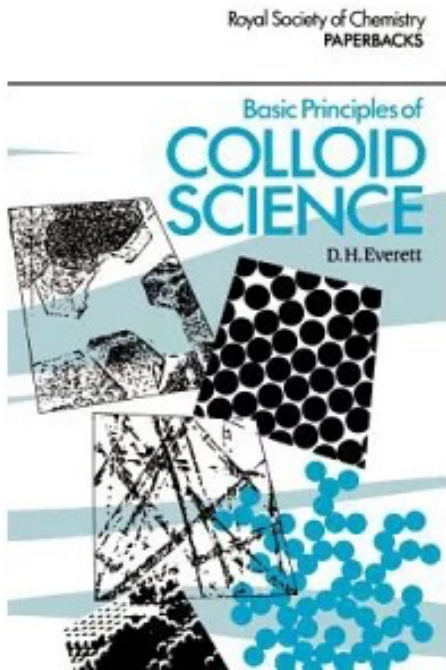
Exp

EIC gives us the opportunity for the physics we are interested in.

Hoping to increase momentum for further discussion.



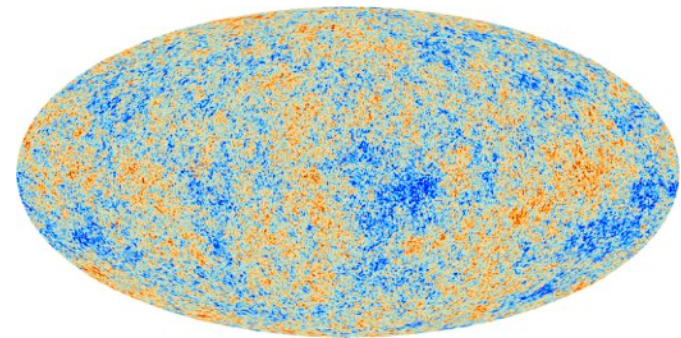
Does our material world prefer non-uniformity rather than uniformity?



Colloid

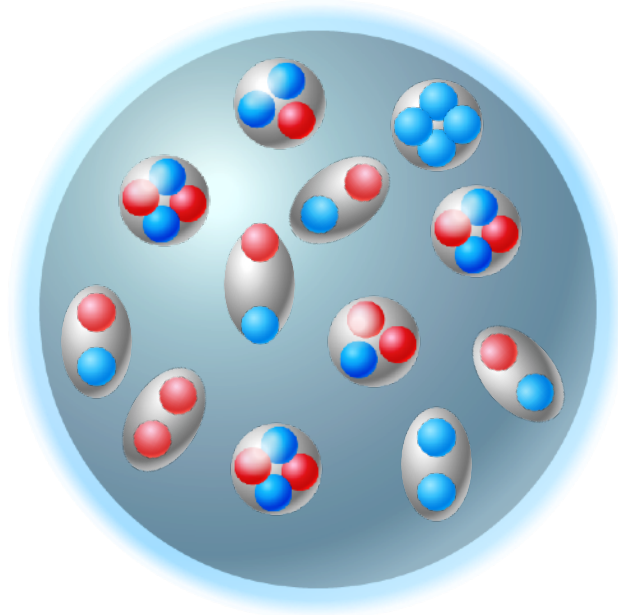


LLPS
Nature (2018-03-15)



CMB
by Planck

Does our **atomic nucleus** prefer non-uniformity rather than uniformity?



Key ideas behind

- Nucleus is not a static, but a dynamic system even in the ground state.
- Minor components sometimes determine the nature of the system.
- Interplay of spin and isospin makes nucleus unique quantum system.

Nuclear force: pion exchange

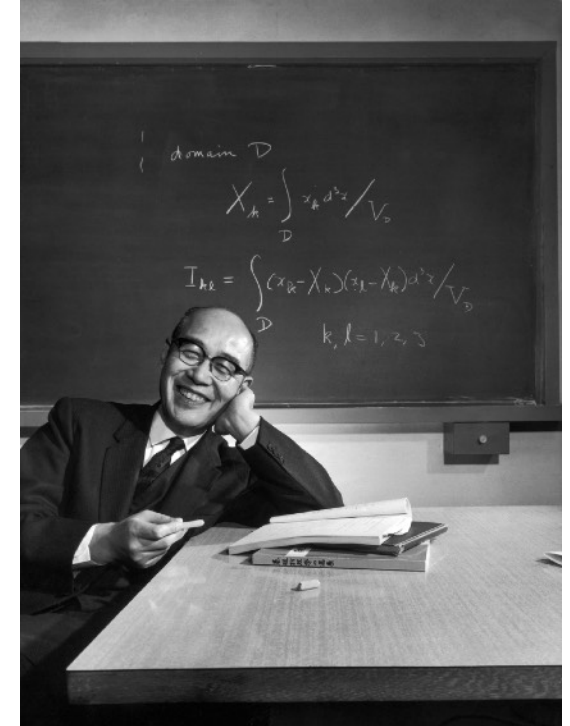
On the Interaction of Elementary Particles. I.

By Hideki YUKAWA.

(Read Nov. 17, 1934)

§ 1. Introduction

Assuming $\lambda = 5 \times 10^{12} \text{cm}^{-1}$, we obtain for m_π a value 2×10^3 times as large as the electron mass. As such a quantum with large mass and positive or negative charge has never been found by the experiment, the above theory seems to be on a wrong line. We can show, however, that, in the ordinary nuclear transformation, such a quantum can not be emitted into outer space.



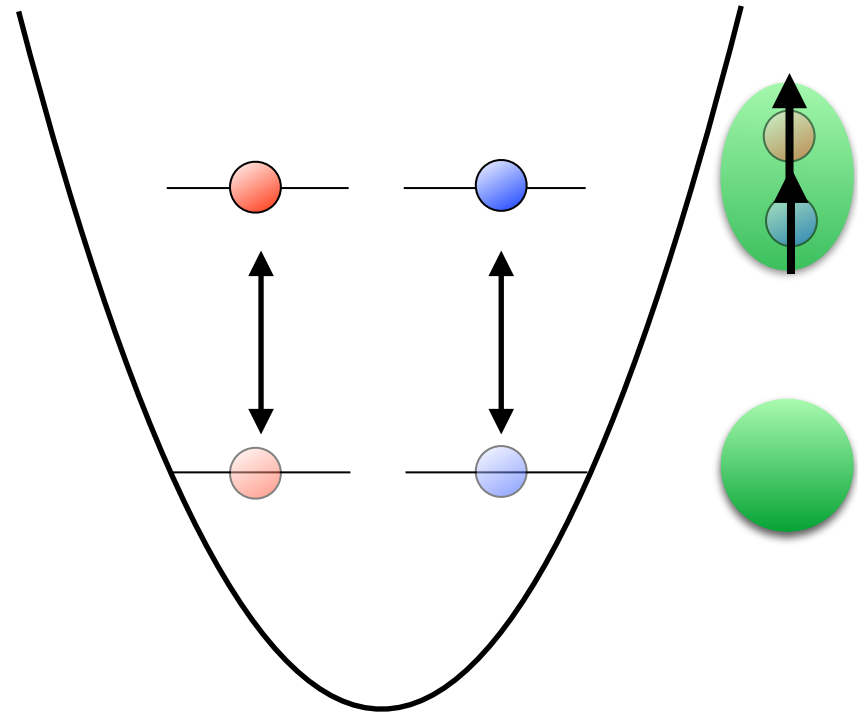
$$V_{12} = m_\pi c^2 \frac{f^2}{4\pi\hbar c^3} (\tau_1 \cdot \tau_2) \times \left[\underbrace{(\sigma_1 \cdot \sigma_2) \frac{e^{-\mu_\pi r}}{4\pi r}}_{\text{centralforce}} + \underbrace{S_{12} \left(1 + \frac{3}{\mu_\pi r} + \frac{3}{(\mu_\pi r)^2} \right) \frac{e^{-\mu_\pi r}}{4\pi r}}_{\text{tensorforce}} \right]$$

Properties characterized by pion exchange

Nucleus is not a static, but a dynamic system even in the ground state.

Quantum mixing between the states above and below the Fermi surface.

Stabilized through the off-diagonal terms of the Hamiltonian.



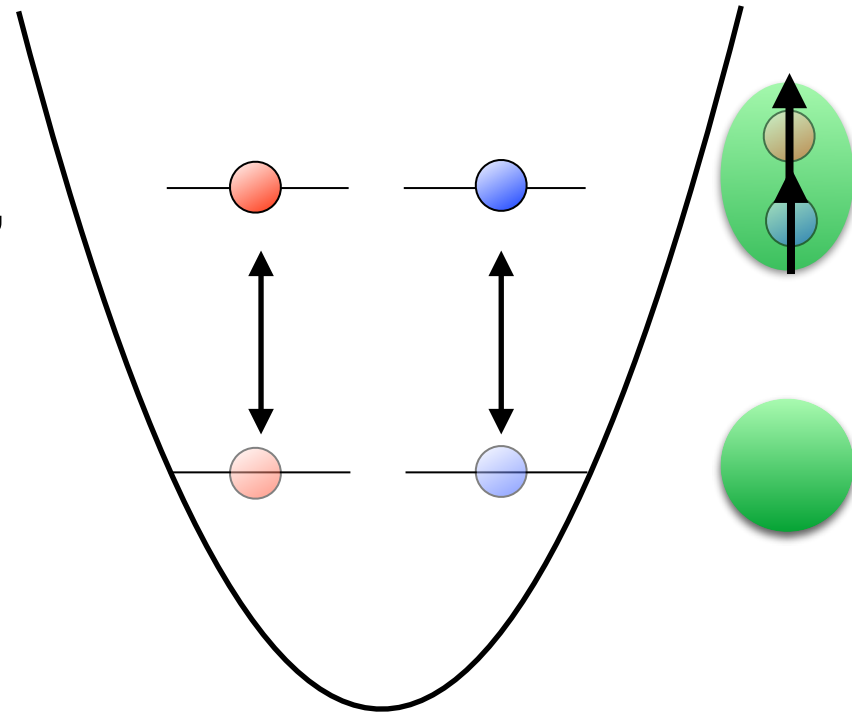
Properties characterized by pion exchange

Minor components sometimes determine the nature of the system.

States above the Fermi surface:

- D state in deuteron
- “High momentum component” in general

A mixture of a few accounts for as much as 50% of the binding energy.



Deuteron cluster plays a significant role.

Properties characterized by pion exchange

Minor components sometimes determine the nature of the system.

States above the Fermi surface:

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A mixture of a few accounts for as much as 50% of the binding energy.

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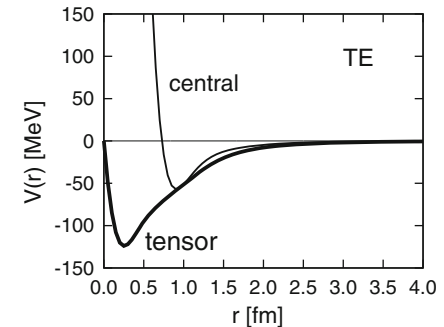
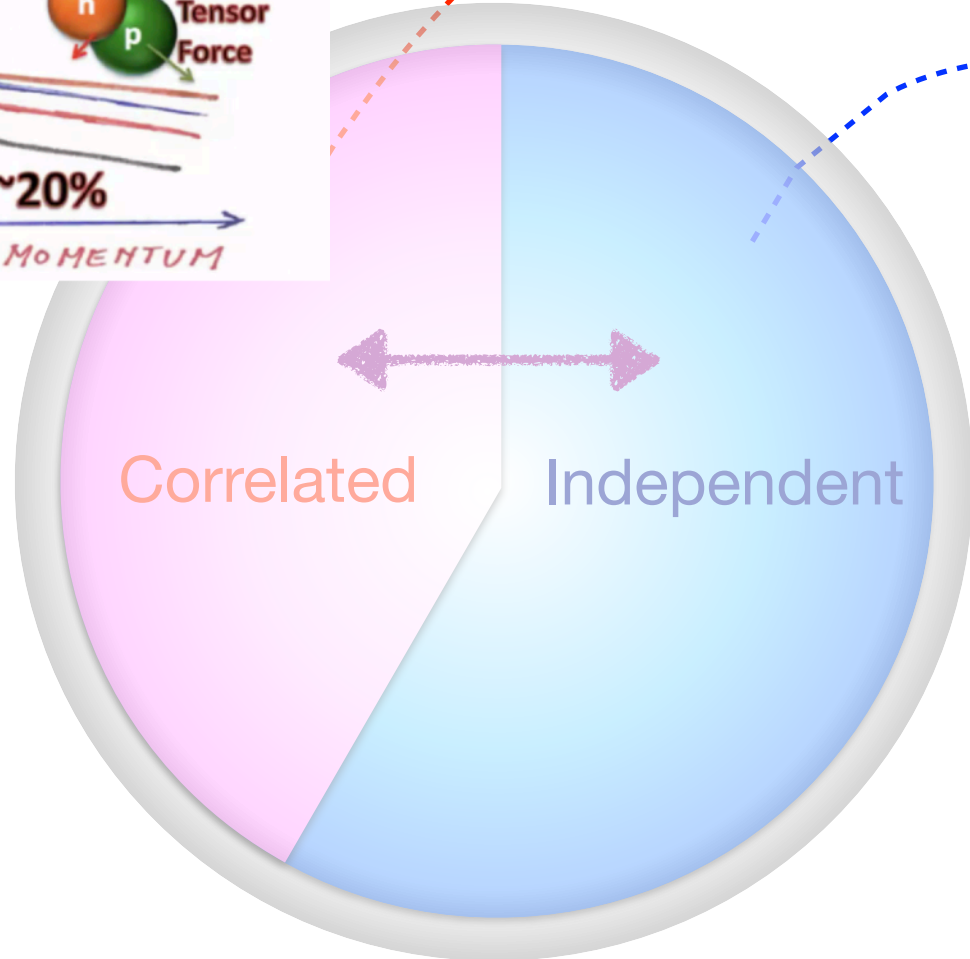
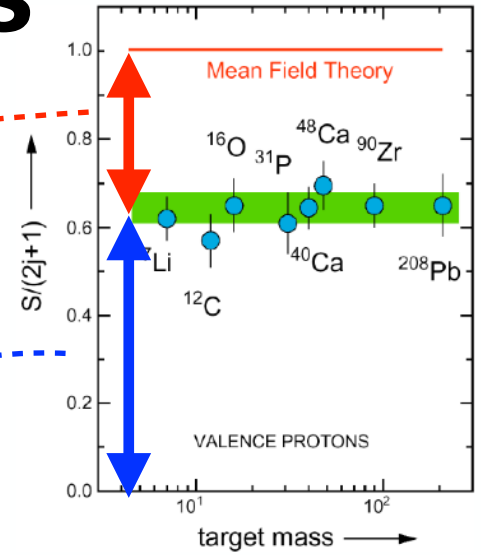
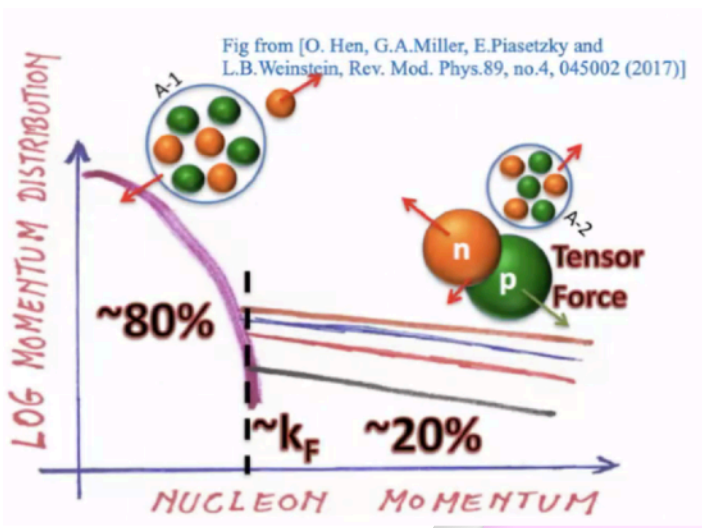


Table 2 Deuteron properties using the AV8' nucleon-nucleon potential.

Energy	-2.24 [MeV]
Kinetic	19.88
(SS)	11.31
(DD)	8.57
Central	-4.46
(SS)	-3.96
(DD)	-0.50
Tensor	-16.64
(SD)	-18.93
(DD)	2.29
LS	-1.02
P(D)	5.78 [%]
Radius	1.96 [fm]
(SS)	2.00 [fm]
(DD)	1.22 [fm]

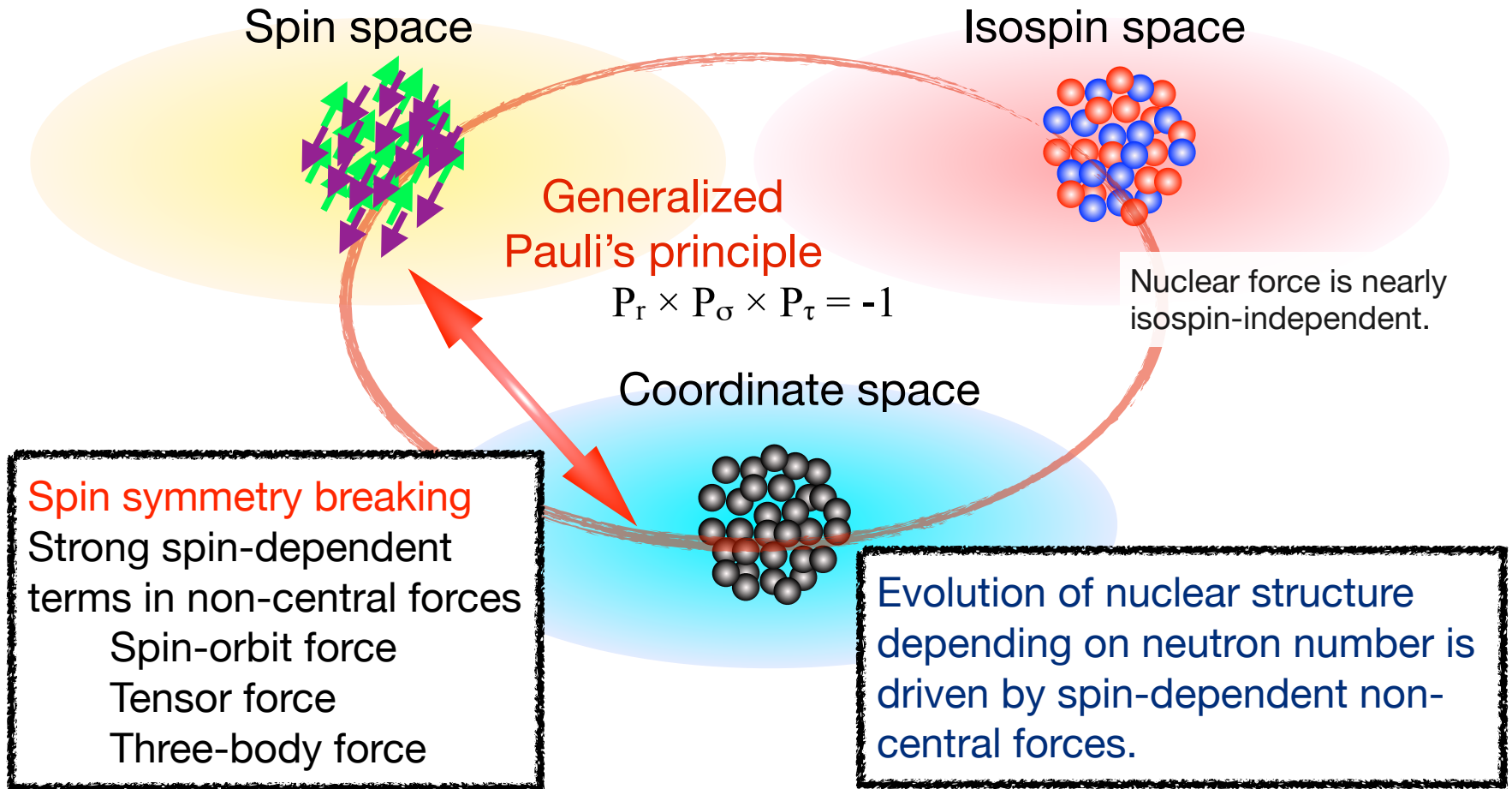
1/3 and 2/3 of the nucleus





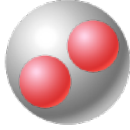
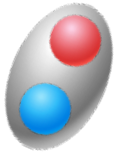
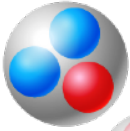

(50)	$g_{9/2}$ (10)	(184)	$d_{3/2}$ (4)
	$p_{1/2}$ (2)		$s_{1/2}$ (2)
	$f_{5/2}$ (6)		$g_{7/2}$ (8)
	$p_{3/2}$ (4)		$d_{5/2}$ (6)
(28)	$f_{7/2}$ (8)		$j_{15/2}$ (16)
			$i_{11/2}$ (12)
(20)	$d_{3/2}$ (4)		$g_{9/2}$ (10)
	$s_{1/2}$ (2)		
	$d_{5/2}$ (6)	(126)	$p_{1/2}$ (2)
			$f_{5/2}$ (6)
(8)			$p_{3/2}$ (4)
			$i_{13/2}$ (14)
			$h_{9/2}$ (10)
			$f_{7/2}$ (8)
(2)		(82)	$h_{11/2}$ (12)
			$d_{3/2}$ (4)
			$s_{1/2}$ (2)
	$p_{3/2}$ (4)		$g_{7/2}$ (8)
	$p_{1/2}$ (2)		$d_{5/2}$ (6)
(2)		(50)	
	$s_{1/2}$ (2)		

Properties characterized by pion exchange

Interplay of spin and isospin makes nucleus unique quantum system.



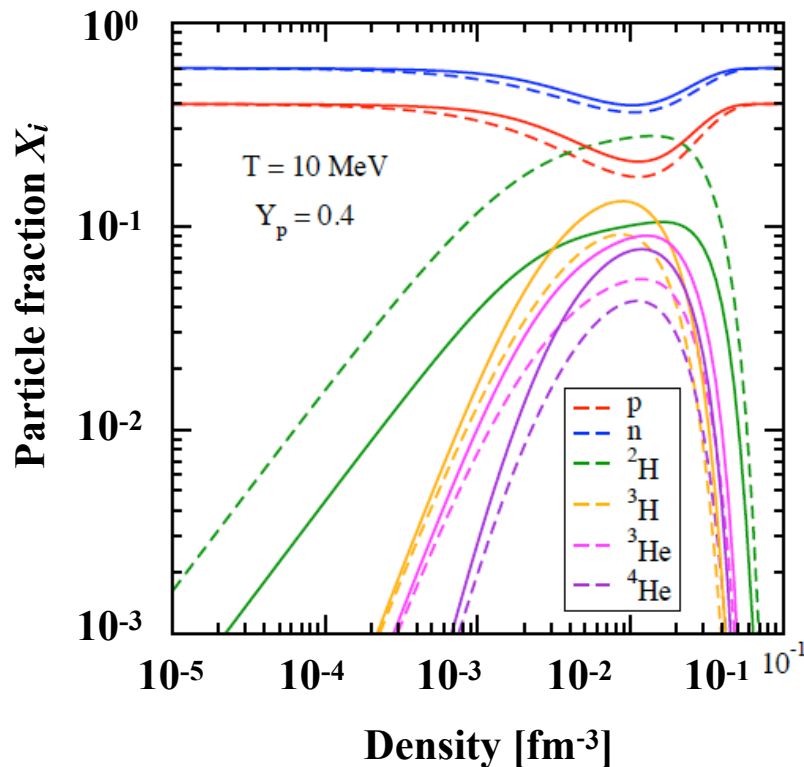
Looking at various clusters simultaneously

		Isospin	
Spin	 α $S=0, T=0$	 n^2 ($T_z=+1$)  p^2 ($T_z=-1$) $S=0, T=1$	
	 d $S=1, T=0$	 t ($T_z=+1/2$)  ${}^3\text{He}$ ($T_z=-1/2$) $S=1/2, T=1/2$	

Progress in theory

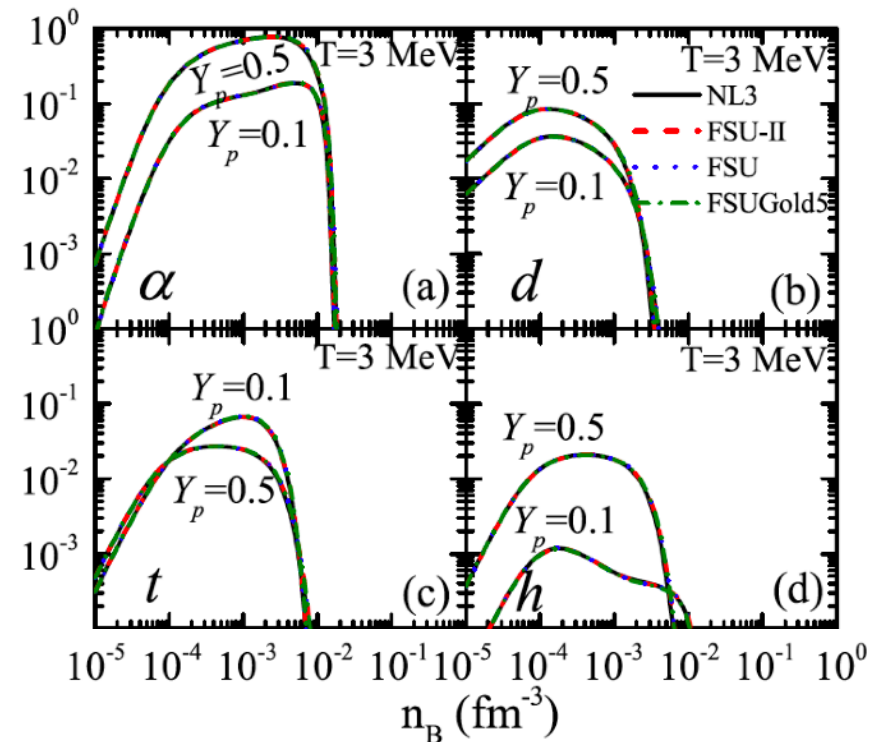
S. Typel,

J. Phys. Conf. Ser. 420, 012078 (2013)



Z.W. Zhang and L.W. Chen

Physical Review C 95, 064330 (2017)



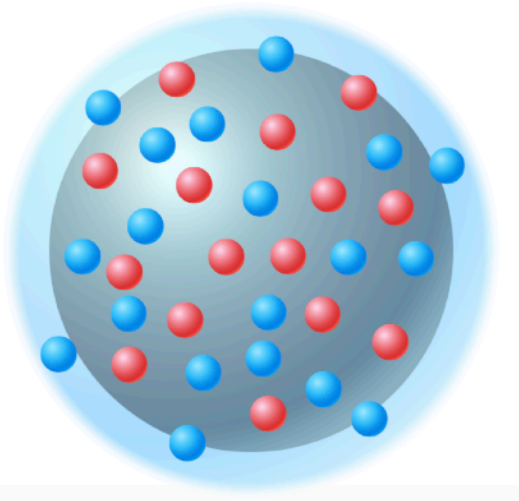
Cluster develops at $< 1/10$ of saturation density

Cluster formation strongly depends on isospin asymmetry

Modern view of atomic nucleus

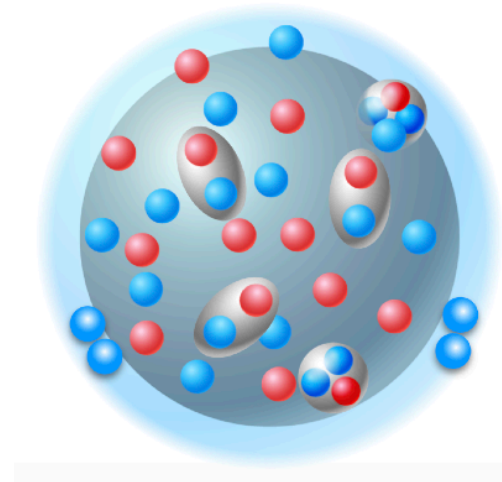
Conventional picture

Uniform nuclei formed by independent neutrons and protons
Limited clusters (such as α) develop only in light and heavy nuclei

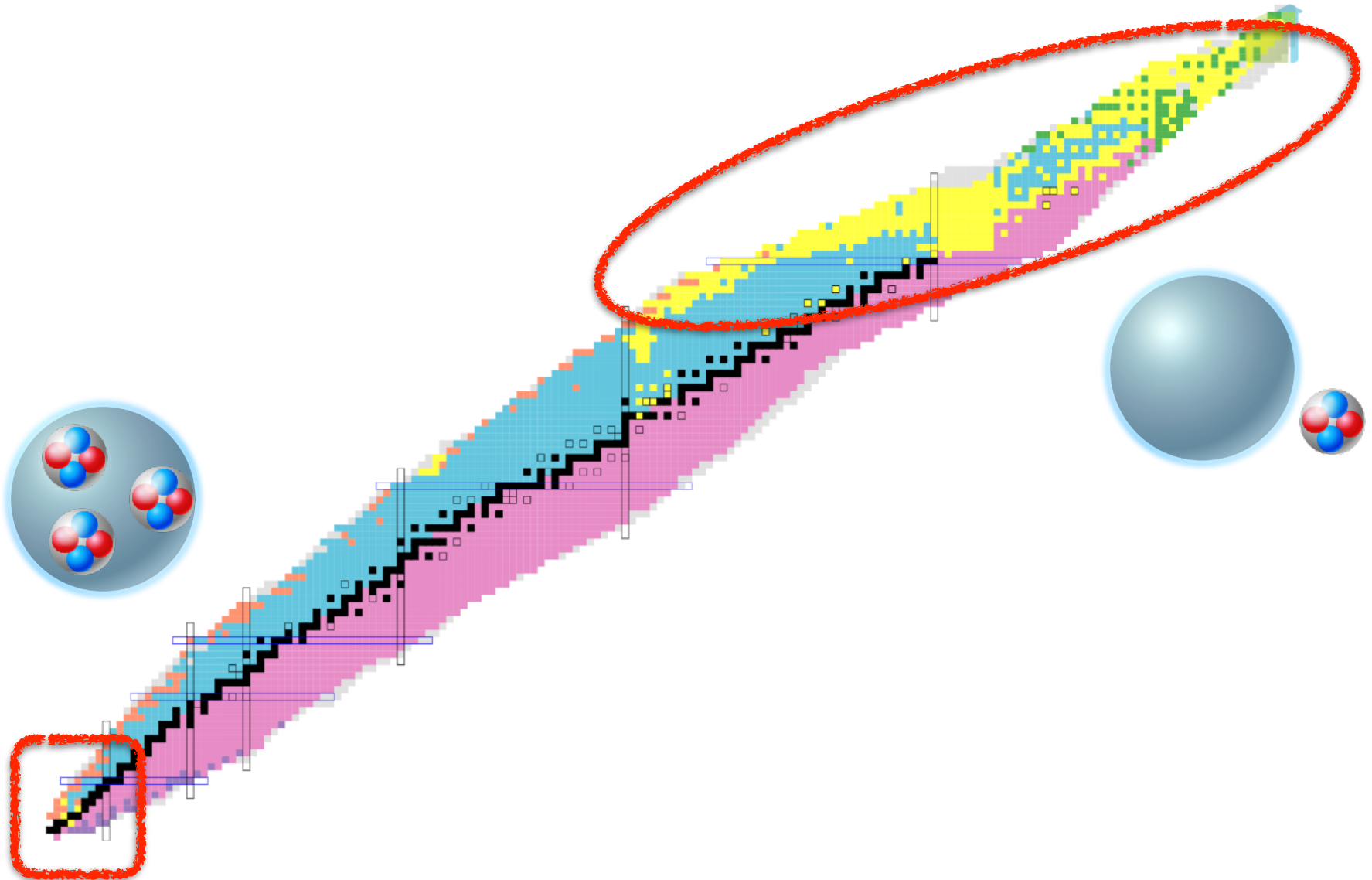


Modern picture

Various clusters (d , t , ${}^3\text{He}$, α , ...) develop in **all nuclei**
Non-uniform nuclei where nucleons and clusters coexist



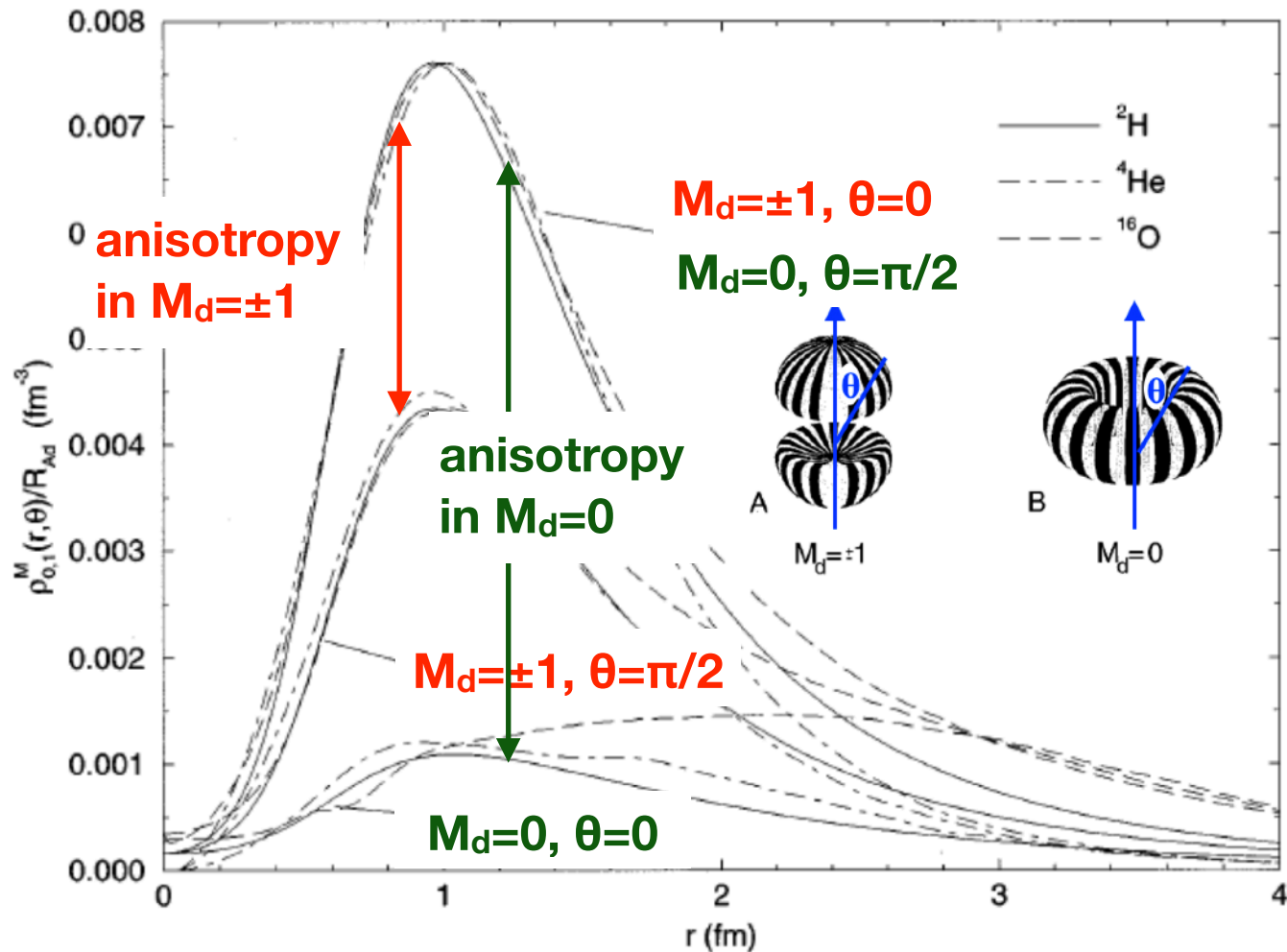
Is nuclear clustering universal?



Deuteron-like spin-dependent anisotropy

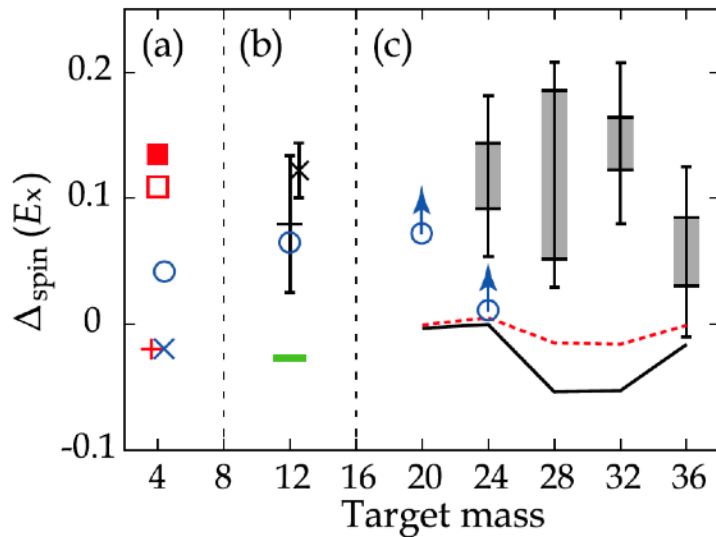
“Femtometer toroidal structures in nuclei”

J. L. Forest et al., Phys. Rev. C **54**, 646 (1996)



Signature of the deuteron cluster?

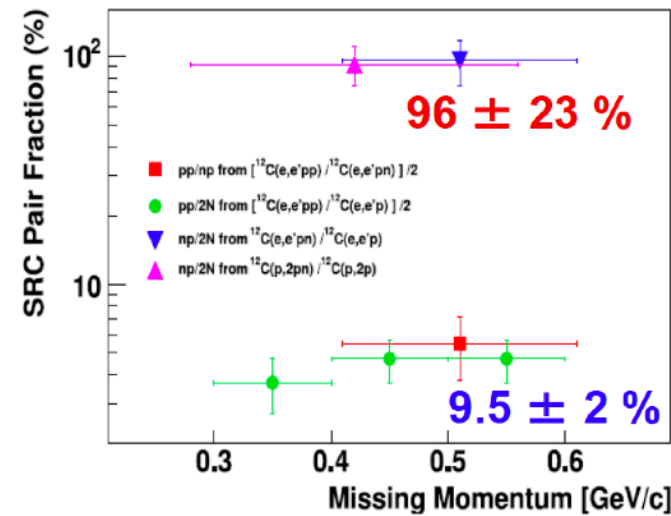
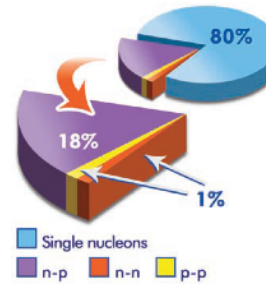
Finite spin expectation value



$$\lim_{E_x \rightarrow \infty} \Delta_{\text{spin}}(E_x) = \langle \vec{S}_p \cdot \vec{S}_n \rangle$$

H. Matsubara et al., Phys. Rev. Lett. **115**, 102501 (2015).

Short range correlation



R. Subedi et al., Science **320**, 1476 (2008)


Knockout reaction $(e, e'p) \rightarrow (p, pN) \rightarrow (p, pX)$

Simple and clean reaction if the quasi-free condition is satisfied.

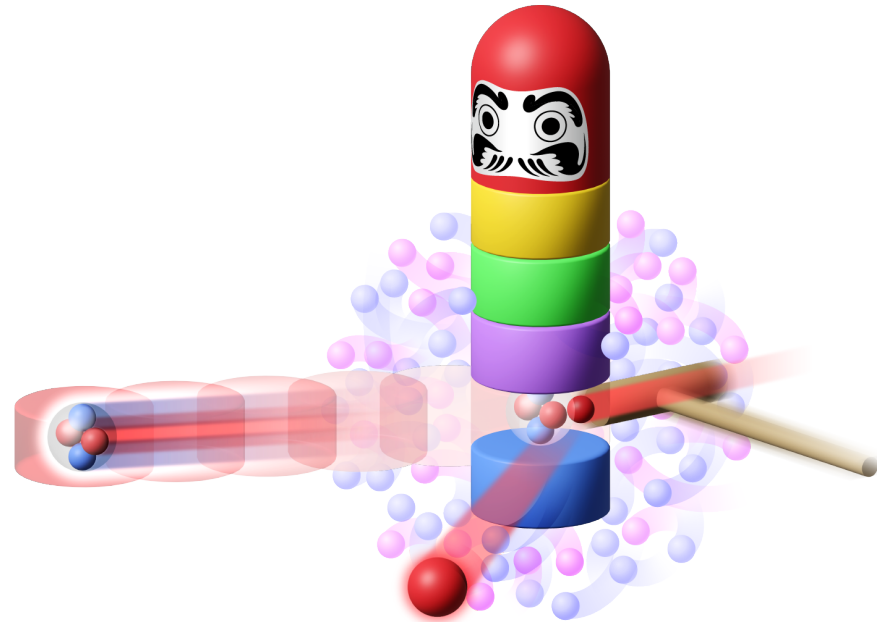
The final state interaction is minimized.

Cluster wave function, momentum distribution can be extracted.

Initial state Cluster Residue

$$|A\rangle = \sum_{i,j} |x\rangle_i \otimes |B\rangle_j$$


Knockout reaction cuts
this entanglement instantly.



ONOKORO Project: cluster knockout

(p, pX) @ $E/A = 200 - 300$ MeV

$X: (p,) d, t, {}^3\text{He}, \alpha$

Relative abundance of each cluster and its isotopic dependence

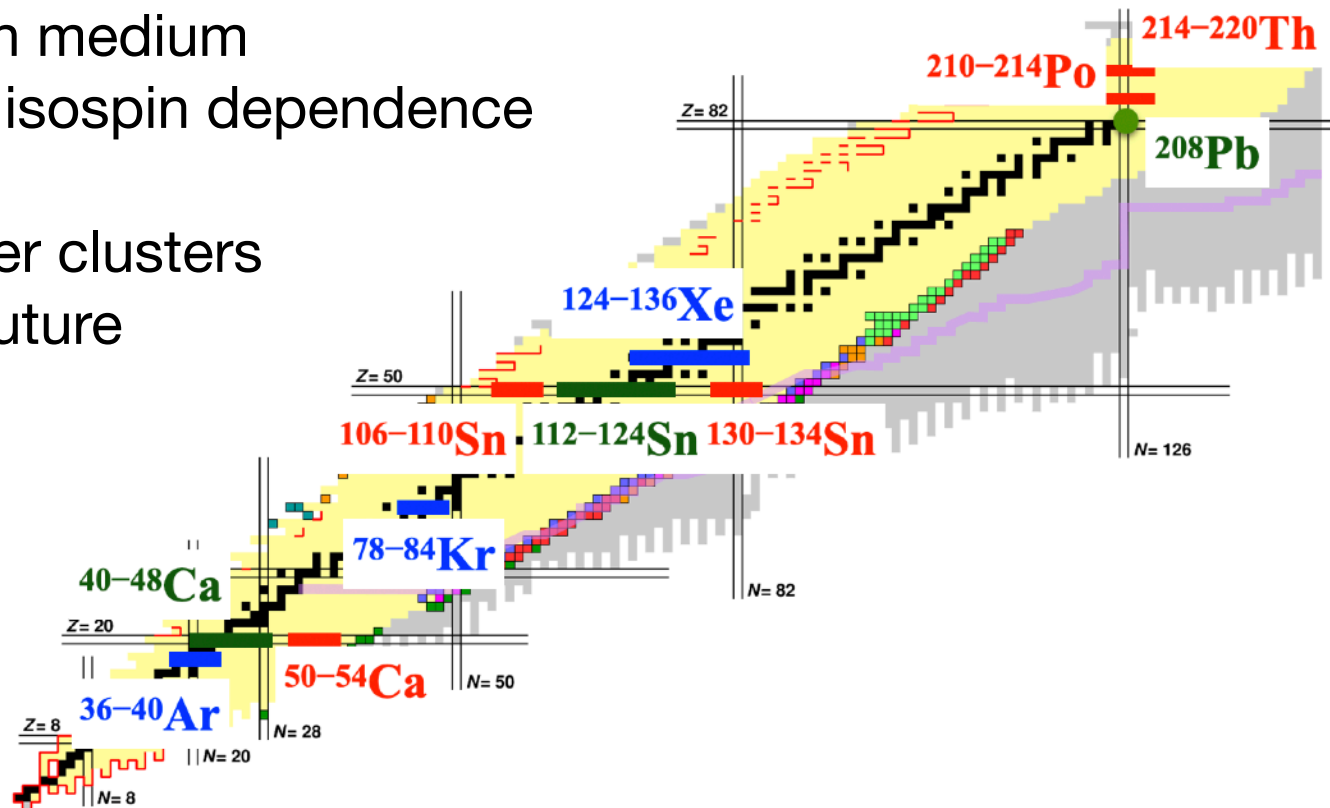
α : Verification of alpha preformation on the surface

d : Tensor force in medium

$t, {}^3\text{He}$: Opposite isospin dependence

Extension to heavier clusters

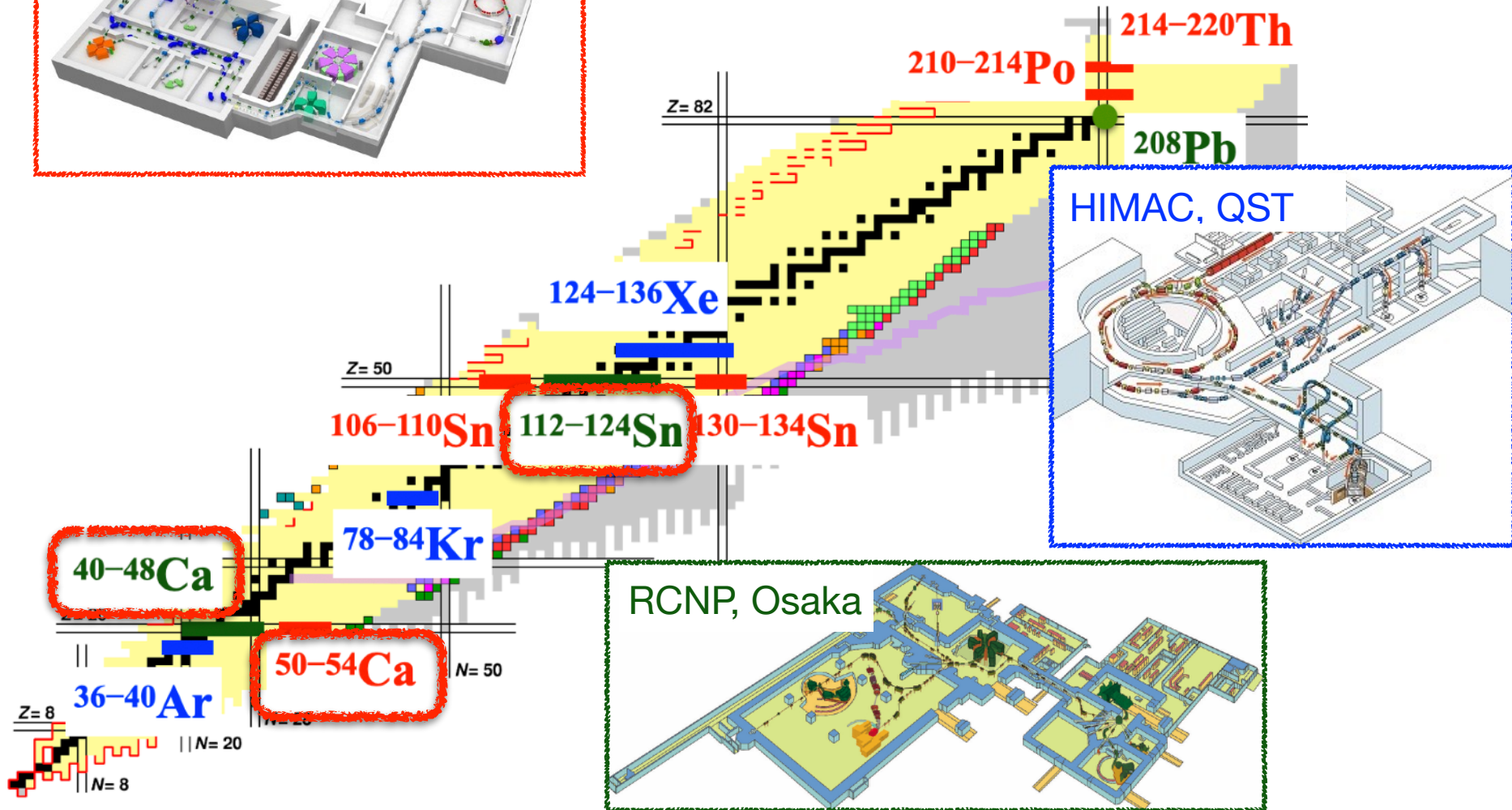
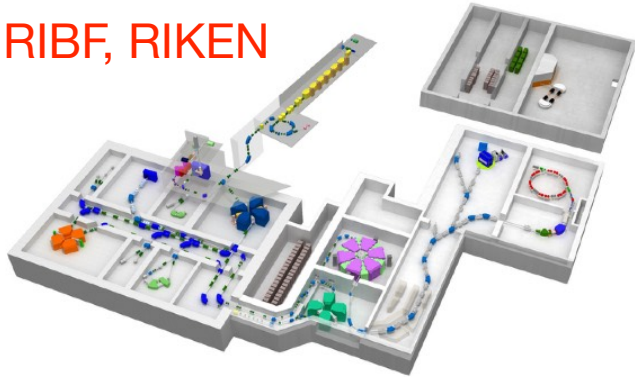
(${}^6\text{He}$, Li, Be, C) in future



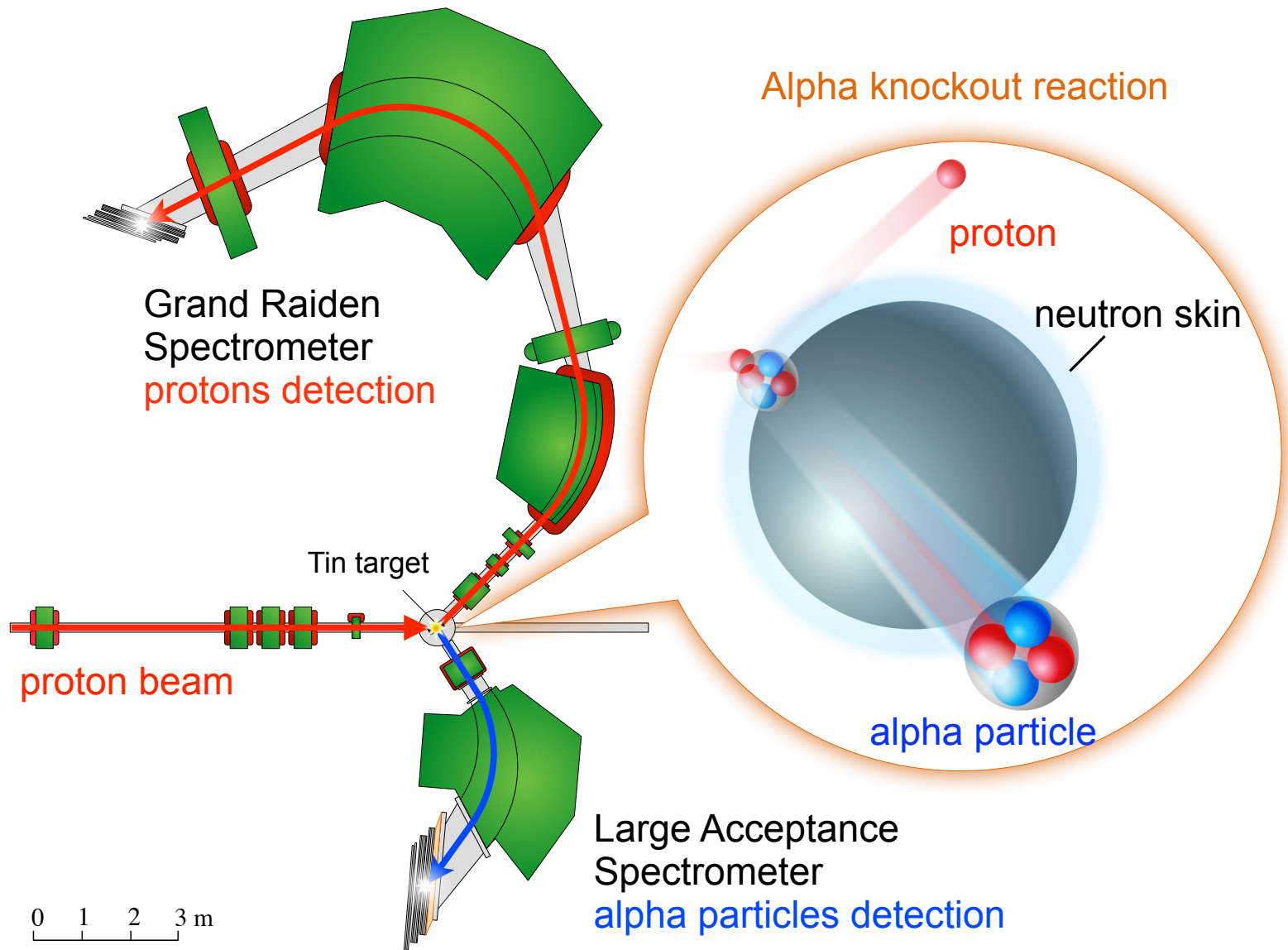
Full use of accelerator facilities in Japan

Wide mass range
Stable and unstable nuclei
Normal and inverse kinematics

RIBF, RIKEN



α clustering in Tin isotopes



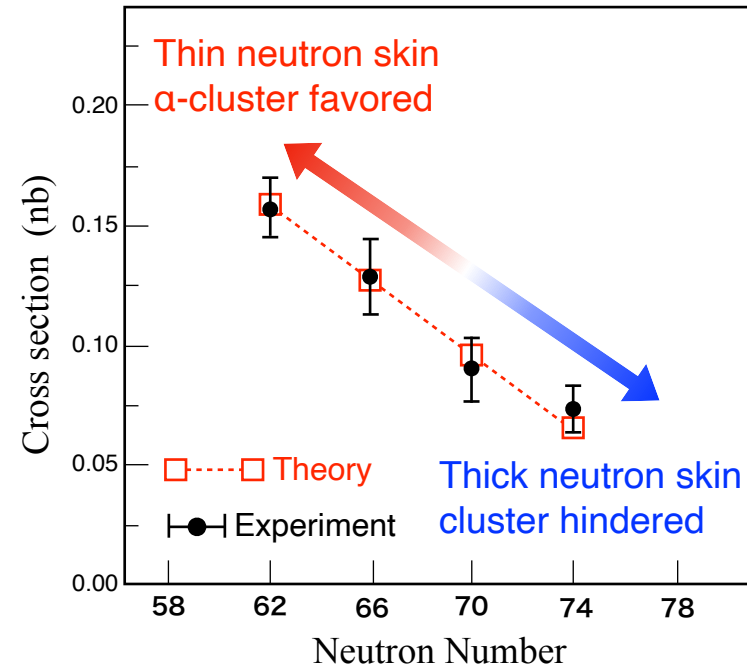
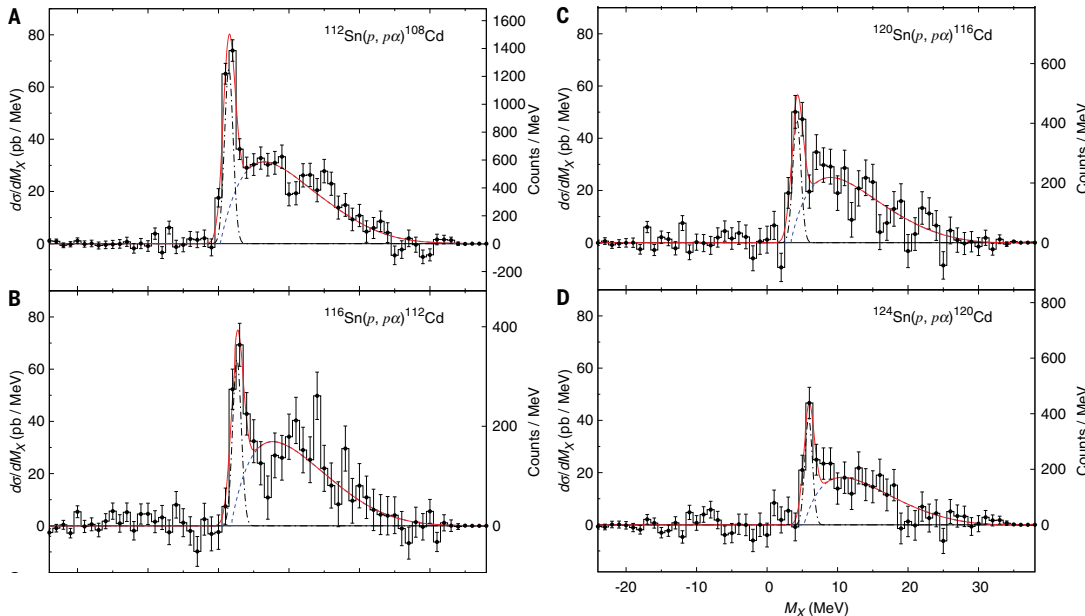
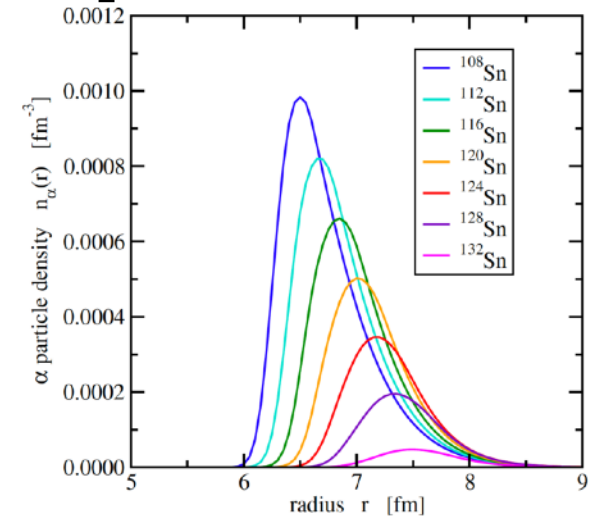
α clustering in Tin isotopes

REPORT

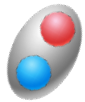
NUCLEAR PHYSICS

Formation of α clusters in dilute neutron-rich matter

Junki Tanaka^{1,2,3*}, Zaihong Yang^{3,4*}, Stefan Typel^{1,2}, Satoshi Adachi⁴, Shiwei Bai⁵, Patrik van Beek¹, Didier Beaumel⁶, Yuki Fujikawa⁷, Jiaying Han⁵, Sebastian Heil¹, Siwei Huang⁵, Azusa Inoue⁴, Ying Jiang⁵, Marco Knösel¹, Nobuyuki Kobayashi⁴, Yuki Kubota³, Wei Liu⁵, Jianling Lou⁵, Yukie Maeda⁸, Yohei Matsuda⁹, Kenjiro Miki¹⁰, Shoken Nakamura⁴, Kazuyuki Ogata^{4,11}, Valerii Panin³, Heiko Scheit¹, Fabia Schindler¹, Philipp Schrock¹², Dmytro Symochko¹, Atsushi Tamii⁴, Tomohiro Uesaka³, Vadim Wagner¹, Kazuki Yoshida¹³, Juzo Zenihiro^{3,7}, Thomas Aumann^{1,2,14}



(p,pX) from Calcium isotopes



$^{40}\text{Ca}(p,pd)$



$^{40}\text{Ca}(p,pt)$

^{40}Ca in July 2023

$^{42,44,48}\text{Ca}$ in March 2024



S_X [MeV]

S_X [MeV]



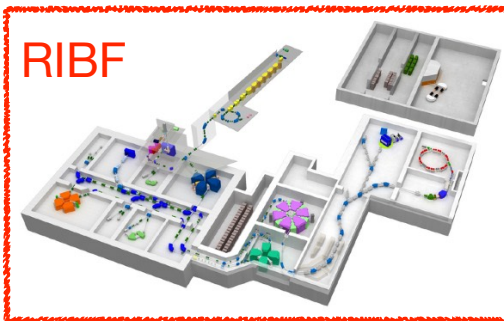
$^{50-52}\text{Ca}$ in Dec. 2024



$^{40}\text{Ca}(p,p^3\text{He})$



$^{40}\text{Ca}(p,p\alpha)$



S_X [MeV]

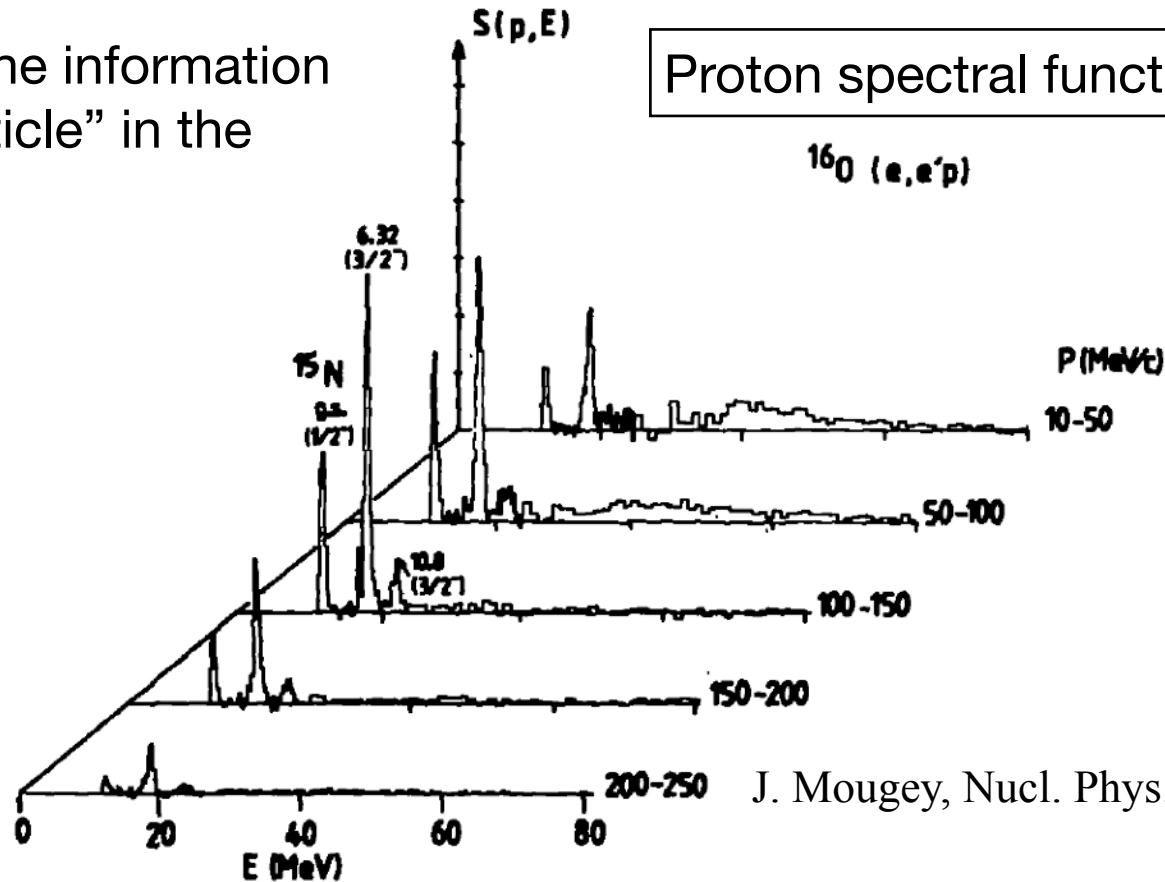
S_X [MeV]

Generalization of the spectral function

Benhar, Fabrocini, Fantoni, Nucl. Phys. A 505 267 (1989)

$$P(S_X, k_F) = \sum_R |\langle R: X(S_X, k_F) | A \rangle|^2 \delta(S_X - E_A - E_R - M_X)$$

It contains all the information about the “particle” in the nucleus.

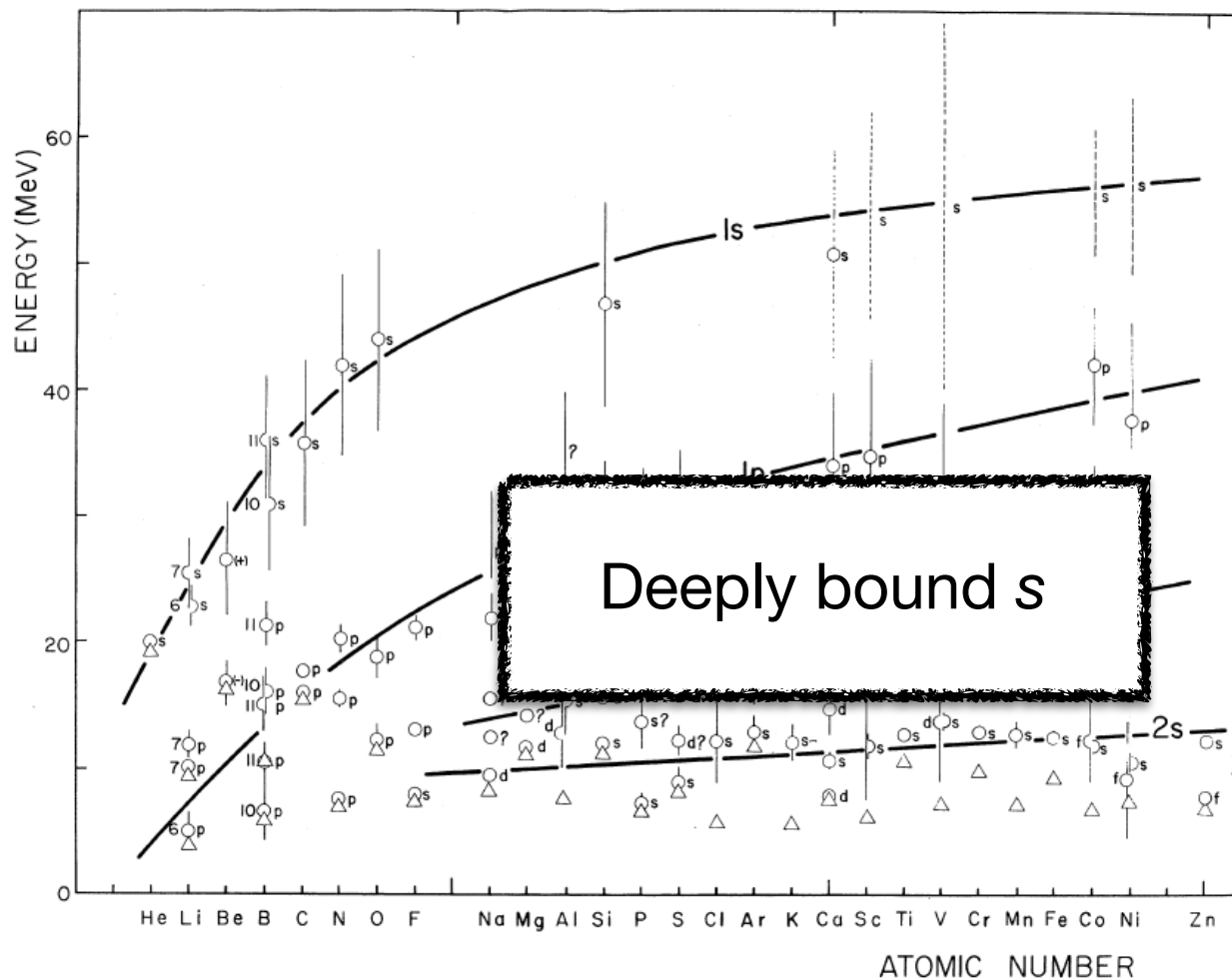


J. Mougey, Nucl. Phys. A 335, 35 (1980)

First determination of the spectral function for clusters

Do clusters form shell structures?

Shell structures seen in $(p,2p)$ measurements



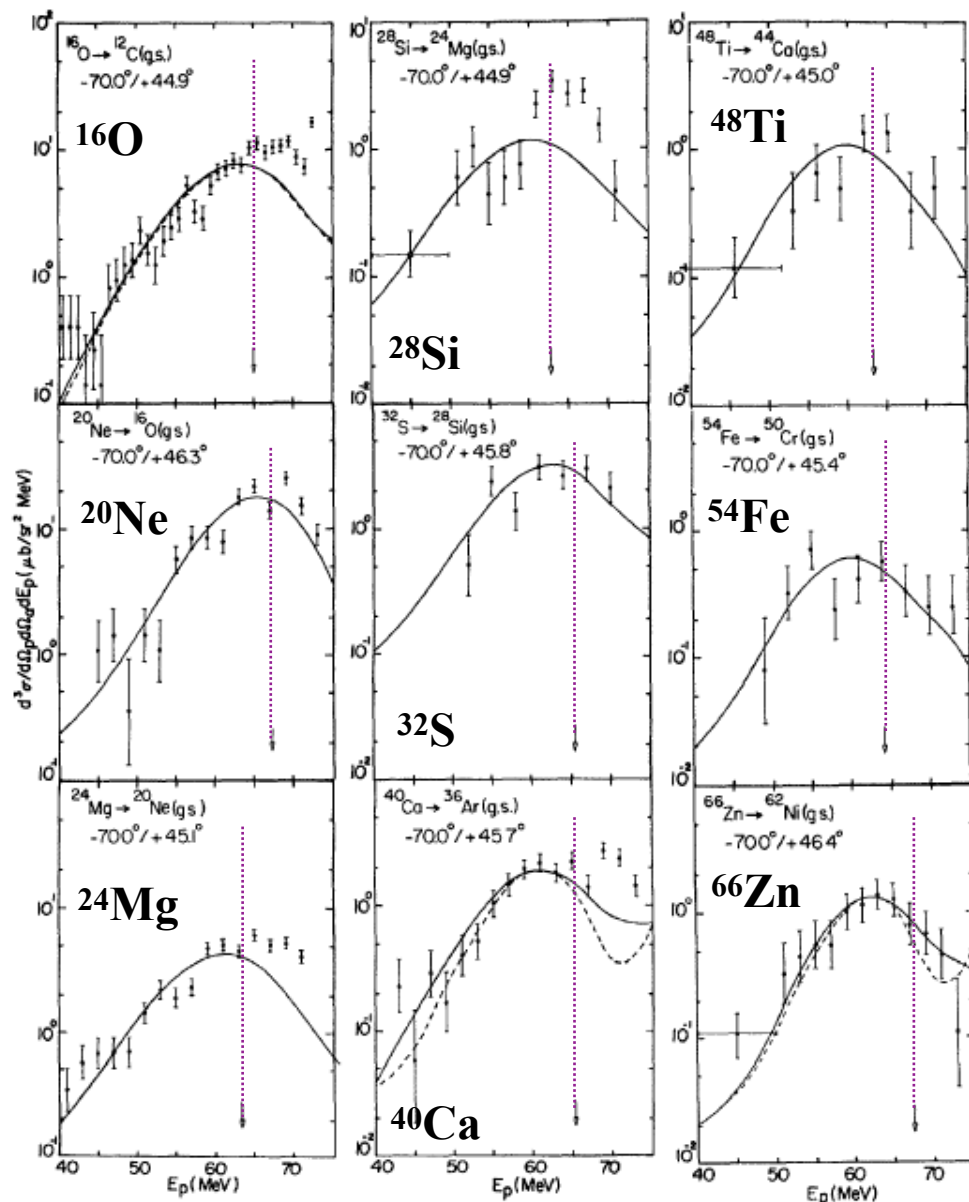
G. Jacob and Th. A. J. Maris, Rev. Mod. Phys. 45, 6 (1973)

Past (p,pX) data shows only S orbitals.

T.A. Carey et al., PRC **29**, 1273 (1984)
($p,p\alpha$) @ 101.5 MeV

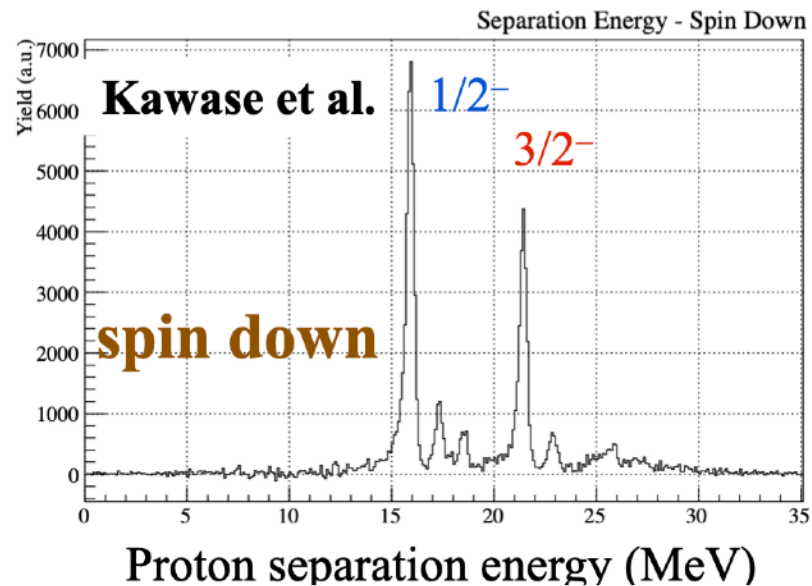
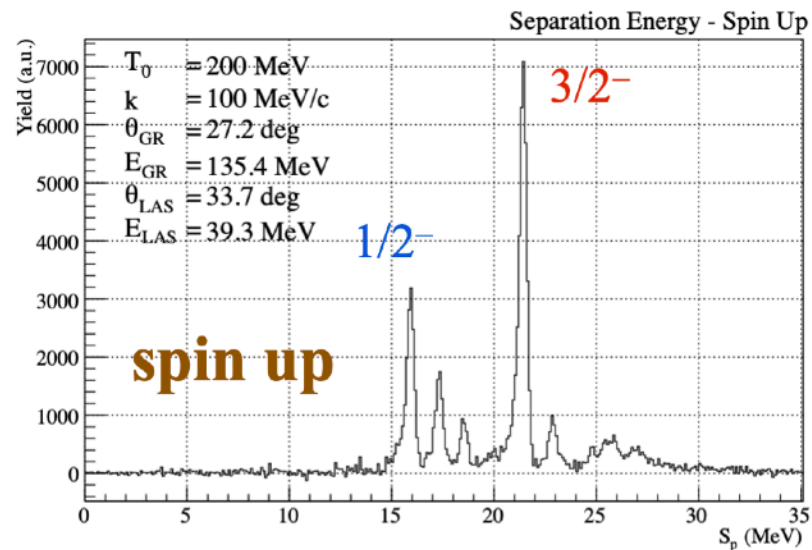
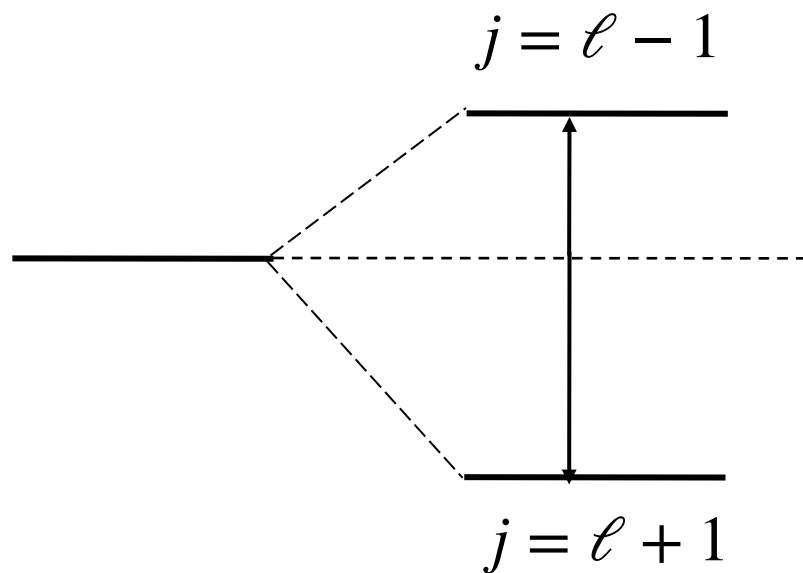
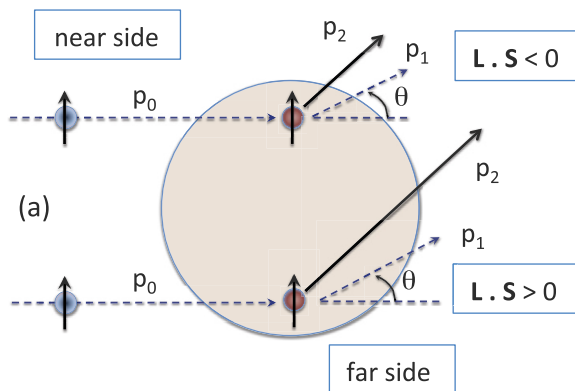
Why?

How about d , t , ^3He ?



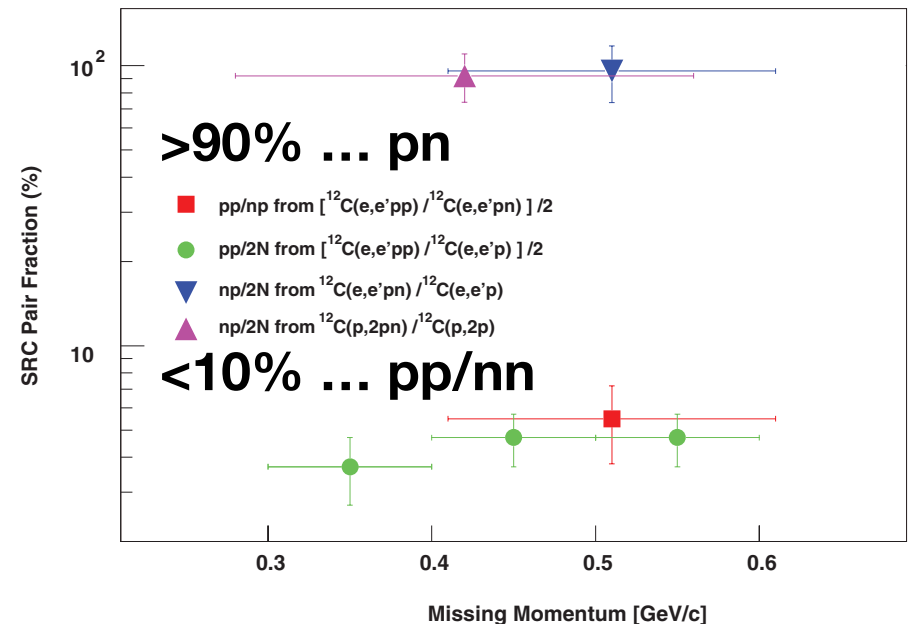
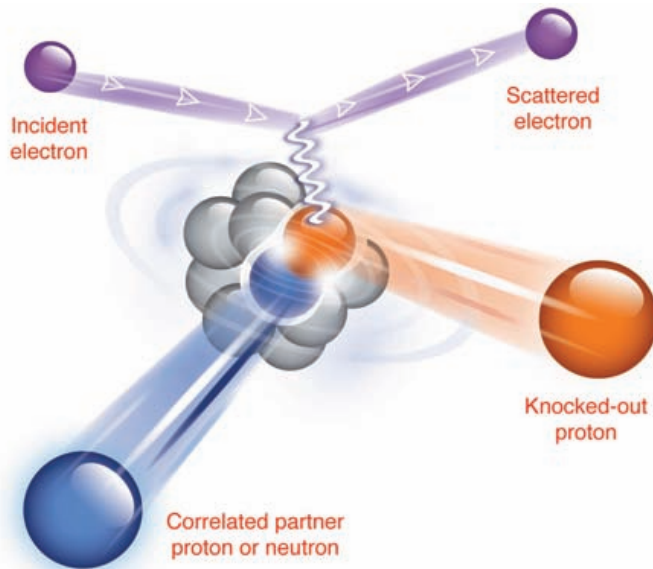
Separation of $J_>$ and $J_<$

Maris effect



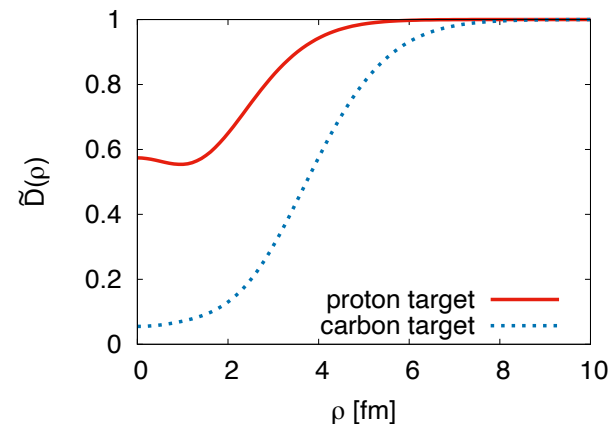
Hot topic: short range correlation

R. Subedi et al., Science **320** 1476 (2008).



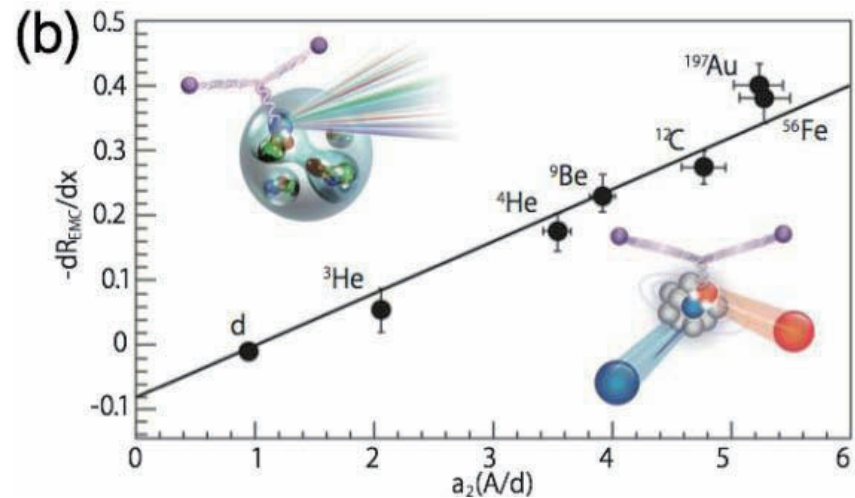
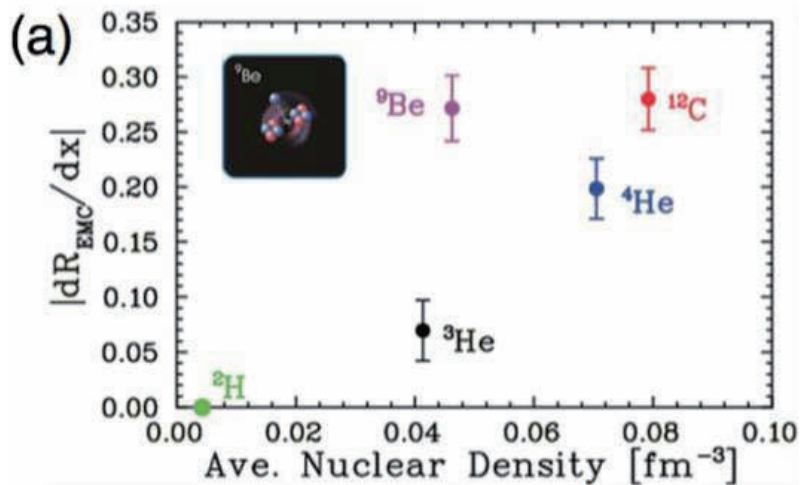
→ **Deuteron (cluster) knockout using electron**

- ☺ Transparent probe
 - ☹ Only applicable to stable nuclei
- c.f. SCRIT



Cluster “size” and EMC effect

EMC effect is determined by the local density, not the average density.

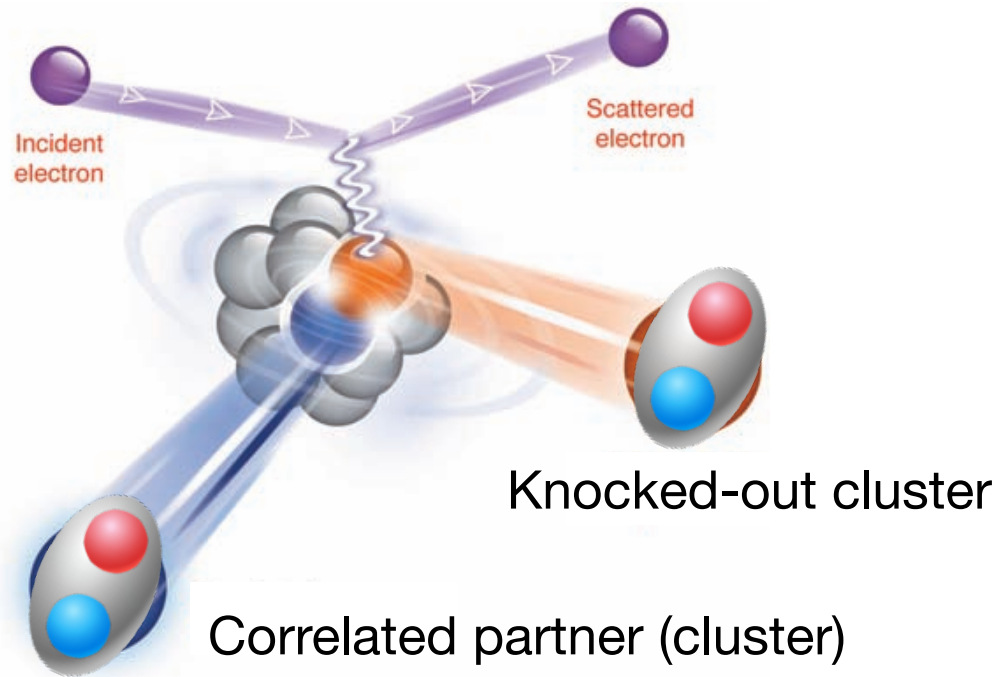


Cluster size and amount play a role.

→ EM form factor of the cluster

“Clusters” made of clusters

$(e, e'XX)$



Clusters may form larger subsystems:
“clusters” made of clusters.

**A clean electron probe is ideal
for studying such “weak” structure.**

Summary

- Variety of topics/programs in the field of low energy nuclear physics.
- EIC gives us the opportunity for the physics we are interested in.
- We hope to increase momentum for further discussion.
- Possible physics cases at EIC:
 - Deeply bound s state.
 - SRC / cluster knockout: $(e, e'X)$
 - EMC effect / EM form factor of the cluster.
 - Cluster-cluster correlation: $(e, e'XX)$.