

Fragmentation functions for EIC

EICで展開する新たな原子核・素粒子物理

Tokyo University, May 28-30, 2024

Ralf Seidl (RIKEN)

QCD at high gluon densities

- Saturation effects

Spin of the nucleon:

- Gluon spin
- Role of Sea quarks

SIDIS
Measurements:
Fragmentation
functions

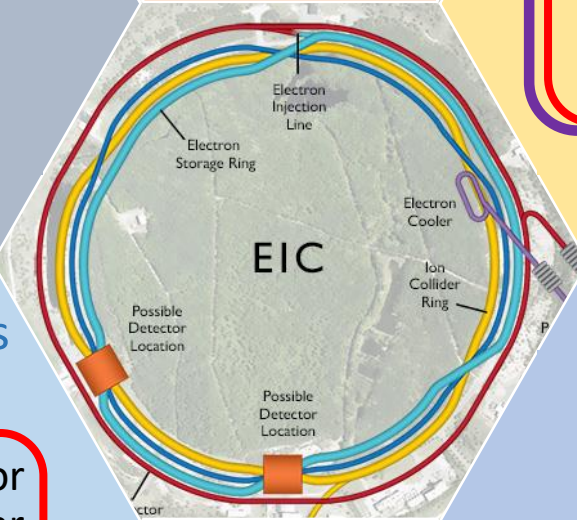
Tomography :

- 3D momentum structure (q, g Sivers, Tensor charge, TMD Evolution)
- 3D spatial structure

Transverse
Momentum
Dependent
PDFs/FFs

Nuclear effects

- Nuclear PDFs
- Passage of color through nuclear matter (nFFs, pT broadening)



Origin of the Mass

- Axial anomaly contributions
- Hadron structure

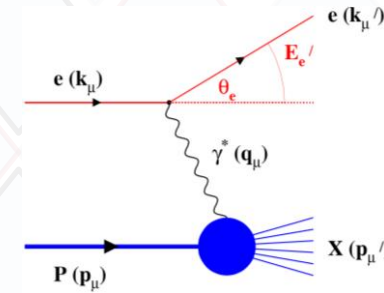
Other

- Spectroscopy (XYZ)
- EW physics
- Fragmentation
- Unpol PDFs

Tools at an EIC and basic requirements

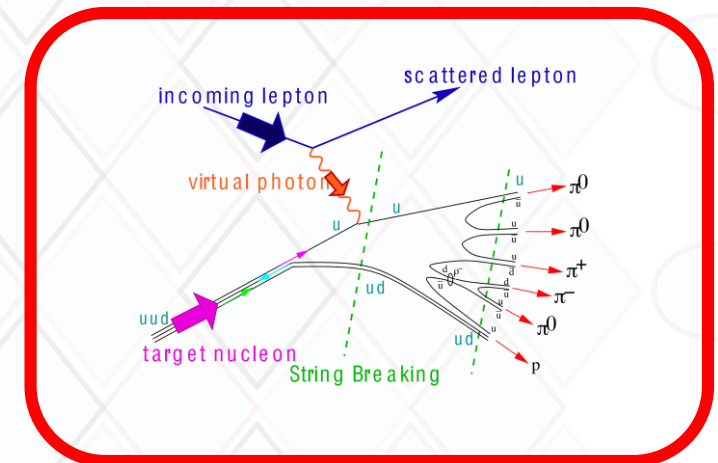
Inclusive Reactions in ep/eA:

- Physics: Structure Fcts.: g_1 , F_2 , F_L
- Very good electron id \rightarrow identify scattered lepton
- Momentum/energy and angular resolution of e' critical
- scattered lepton \rightarrow kinematics of event (x, Q^2)



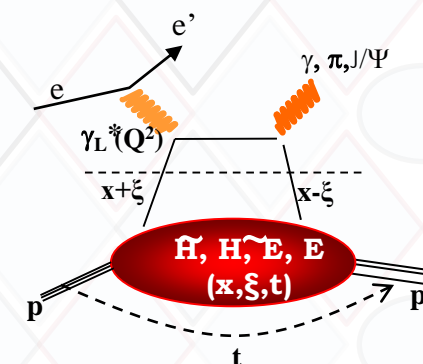
Semi-inclusive Reactions in ep/eA:

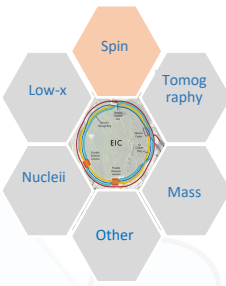
- Physics: TMDs, Helicity PDFs, FF \rightarrow flavor separation, dihadron-corr.,...
 \rightarrow Pion, Kaon asymmetries, cross sections
- Excellent particle ID: π^\pm, K^\pm, p^\pm separation over a wide range in $-3 < \eta < 3$
 \rightarrow excellent p resolution at forward rapidities
- TMDs: full Φ -coverage around γ^* , wide p_t coverage
- Excellent vertex resolution \rightarrow Charm, Bottom separation



Exclusive Reactions in ep/eA:

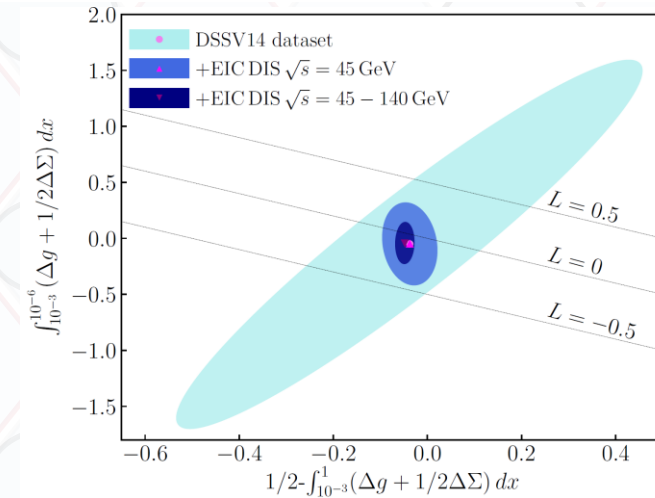
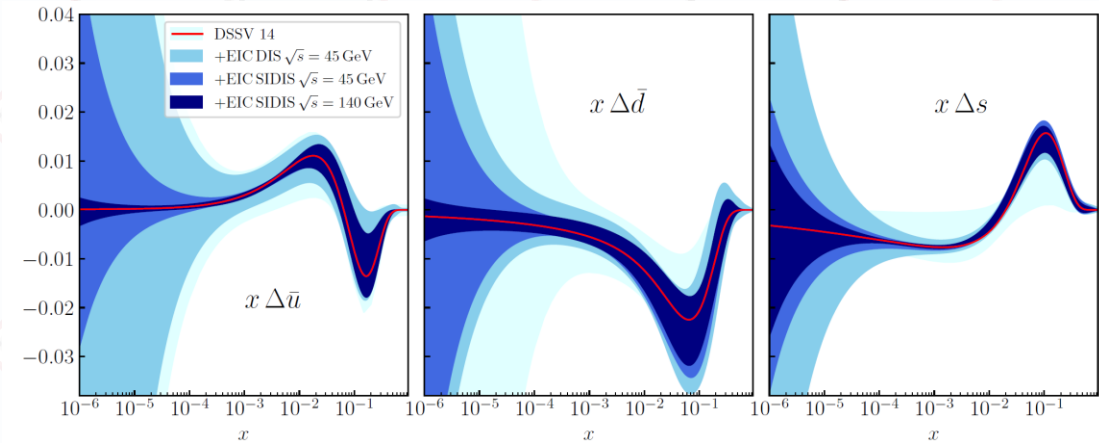
- Physics: DVCS, excl. VM/PS prod. \rightarrow GPDs, parton imaging in b_T ; $g(x, Q^2, b_T)$
- Exclusivity \rightarrow large rapidity coverage \rightarrow rapidity gap events
 \searrow reconstruction of all particles in event
- high resolution, wide coverage in $t \rightarrow b_t \rightarrow$ Roman pots
- eA: veto nucleus breakup, determine impact parameter of collision
 \rightarrow acceptance for neutrons in ZDCs





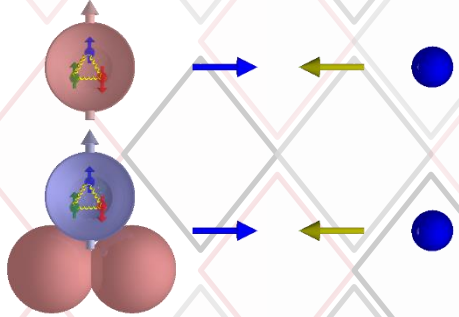
Gluon and sea polarization

- 1 year of EIC running will pin down gluon polarization
- Using SIDIS: precise determination of sea quark helicities, especially **strange** contribution of interest
- Indirect determination of orbital angular momentum via sum rule
- Also interesting access to flavor via charged current reactions

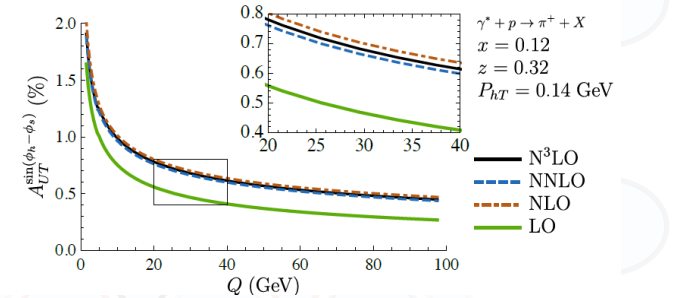
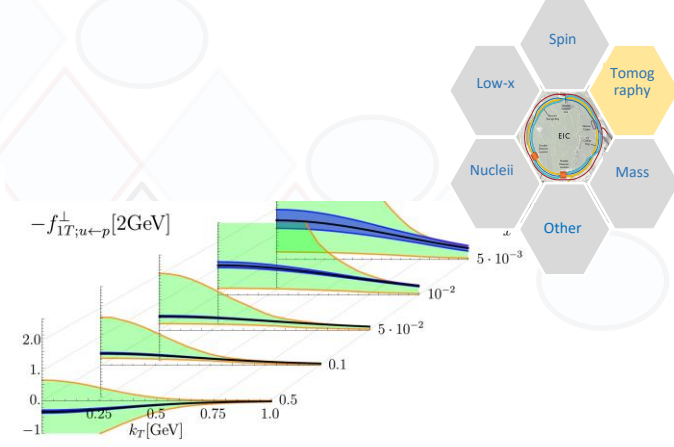


[PRD 102 \(2020\), 094018](#)

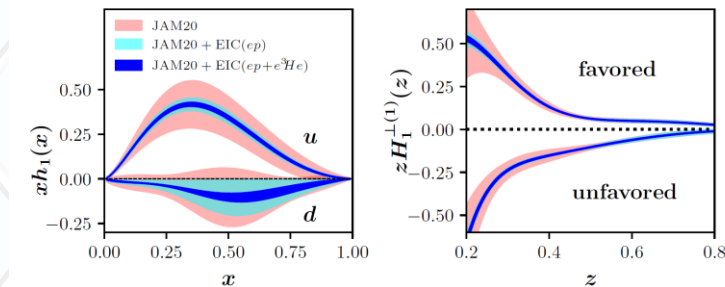
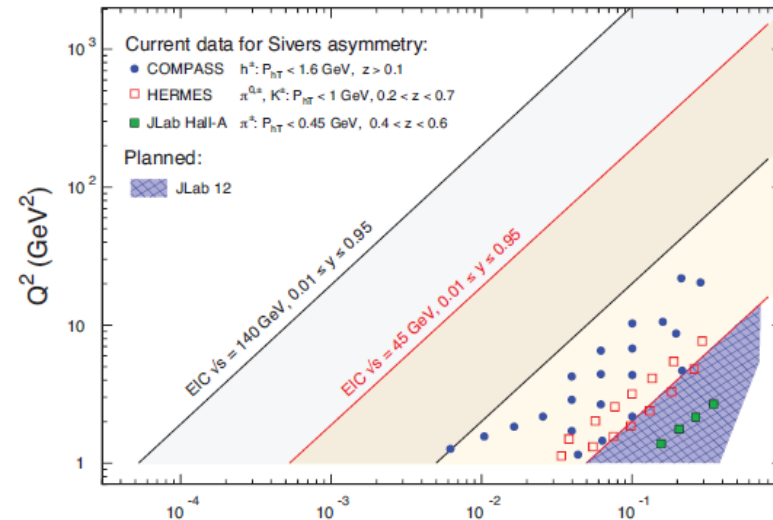
EIC TMD Goals: 3D Transverse spin and momentum structure



Deliverables	Observables	What we learn	Stage I	Stage II
Sivers & unpolarized TMD quarks and gluon	SIDIS with Transverse polarization; di-hadron (di-jet)	Quantum Interference & Spin-Orbital correlations	3D Imaging of quarks valence+sea	3D Imaging of quarks & gluon; Q^2 (P_{hT}) range QCD dynamics
Chiral-odd functions: Transversity; Boer-Mulders	SIDIS with Transverse polarization	3 rd basic quark PDF; novel hadronization effects	valence+sea quarks	Q^2 (P_{hT}) range for detailed QCD dynamics



Tables from original EIC white paper

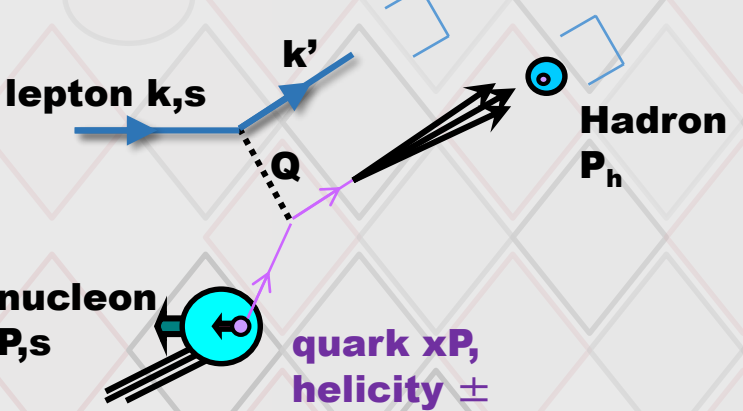


Current coverage for transverse spin related SIDIS measurements

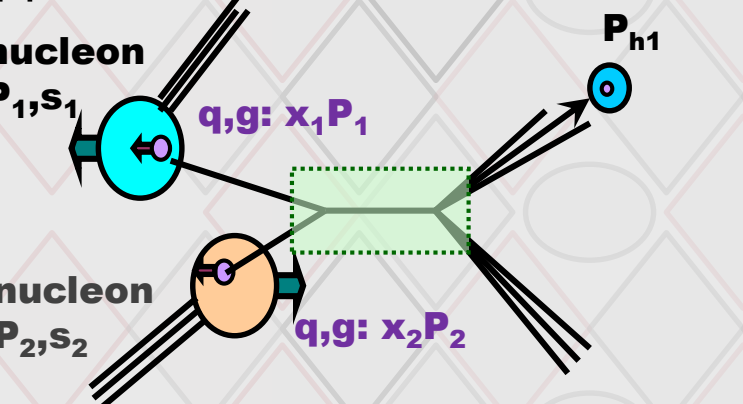
Help of Fragmentation Functions (FF) for nucleon (spin, transverse) structure

- Correlate a hadron in the final state with the struck parton:
 - Parton flavor (HF, favored vs disfavored, strange fragmentation, etc; ie: u quark into a π^+ is **favored**, d quark **disfavored**, s, ubar quarks **favored** in K^+ fragmentation)
 - Spin of the struck quark (Collins and Interference Fragmentation, other polarized FFs)
 - Transverse momentum of struck parton (though convolution with fragmentation transverse momentum)
- Closely related to confinement mechanism

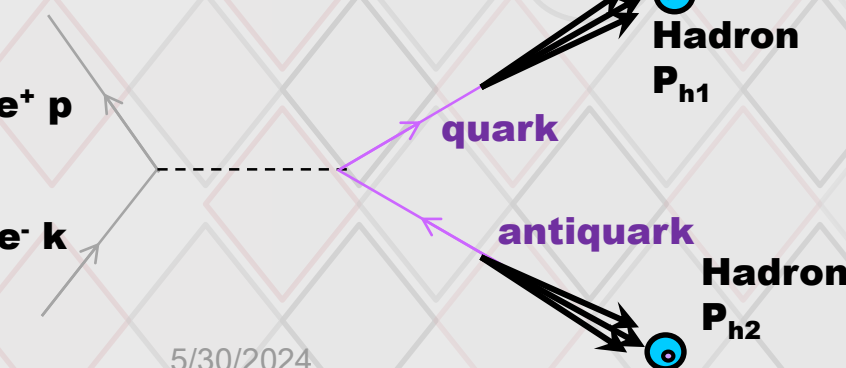
SIDIS



pp collisions



e+e- Annihilation



5/30/2024

Access to Fragmentation functions

- SIDIS:

$$\sigma^h(x, z, Q^2, P_{h\perp}) \propto \sum_q e_q^2 q(x, p_t, Q^2) D_{1,q}^h(z, k_t, Q^2)$$
 - Relies on unpol PDFs
 - Parton momentum known at LO
 - Flavor structure directly accessible
 - Transverse momenta convoluted between FF and PDF
- pp:

$$\sigma^h(P_T) \propto \int_{x_1, x_2, z} \sum_{a, a' \in q, g} f_a(x_1) \otimes f_{a'}(x_2) \otimes \sigma_{aa'} \otimes D_{1,q}^h(z)$$
 - Relies on unpol PDFs
 - leading access to gluon FF
 - Parton momenta not directly known
- e+e-:

$$\sigma^h(z, Q^2, k_t) \propto \sum_q e_q^2 (D_{1,q}^h(z, k_t, Q^2) + D_{1,\bar{q}}^h(z, k_t, Q^2))$$
 - No PDFs necessary
 - Clean initial state, parton momentum known at LO
 - Flavor structure not directly accessible*



Single hadron FF


Unpolarized ingredients	Polarized ingredients	Flavor sensitivity
Single hadron cross sections: $e^+e^- \rightarrow hX$ $D_{1,q}^h(z, Q^2)$ <div style="background-color: #d9ead3; padding: 5px; margin-top: 10px;"> PRL111 (2013) 062002 PRD101(2020) 092004 </div>	Azimuthal asymmetries: $e^+e^- \rightarrow (h)(h)X,$ $\cos(\phi_1 + \phi_2)$ $H_{1,q}^{\perp(1)h}(z, Q^2)$ <div style="background-color: #d9ead3; padding: 5px; margin-top: 10px;"> PRL 96 (2006) 232002 PRD 78 (2008) 032011 </div>	Unpol SIDIS, pp: $\frac{d\sigma}{dz}$ $e^+e^- \rightarrow (h)(h)X$ <div style="background-color: #d9ead3; padding: 5px; margin-top: 10px;"> PRD92 (2015) 092007 PRD101(2020) 092004 and scale dependence </div>
Transverse momentum dependent FFs: $e^+e^- \rightarrow (h)X$ $D_{1,q}^h(z, k_T, Q^2)$ <div style="background-color: #d9ead3; padding: 5px; margin-top: 10px;"> PRD 99 (2019) 112006 </div>	Transverse momentum dependent asymmetries $e^+e^- \rightarrow (h)(h)X,$ $\cos(\phi_1 + \phi_2), Q_t$ $H_{1,q}^{\perp h}(z, k_T, Q^2)$ <div style="background-color: #d9ead3; padding: 5px; margin-top: 10px;"> PRD100 (2019) 92008 </div>	Polarizing Λ fragmentation <div style="background-color: #d9ead3; padding: 5px; margin-top: 10px;"> PRL 122 (2019), 042001 $D_{1,q}^{\perp h}(z, k_T, Q^2)$ </div>



Dihadron FF (IFF)

Unpolarized ingredients	Polarized ingredients	Flavor sensitivity
Dihadron cross sections $e^+e^- \rightarrow (hh)X$ $D_{1,q}^{h_1 h_2}(z, m, Q^2)$ <div style="background-color: #d9ead3; padding: 5px; margin-top: 10px;"> PRD96 (2017) 032005 </div>	Azimuthal asymmetries: $e^+e^- \rightarrow (hh)(hh)X,$ $\cos(\phi_1 + \phi_2),$ $H_{1,q}^{h_1, h_2, \triangleleft}(z, Q^2, M_h)$ <div style="background-color: #d9ead3; padding: 5px; margin-top: 10px;"> PRL107 (2011) 072004 </div>	Unpol SIDIS, pp: $\frac{d^2\sigma}{dzdm}$

Single hadron measurements

Unpolarized ingredients	Polarized ingredients	Flavor sensitivity
Single hadron cross sections: $e^+e^- \rightarrow hX$ $D_{1,q}^h(z, Q^2)$	Azimuthal asymmetries: $e^+e^- \rightarrow (h)(h)X,$ $\cos(\phi_1 + \phi_2)$ $H_{1,q}^{\perp(1)h}(z, Q^2)$	Unpol SIDIS, pp: $\frac{d\sigma}{dz}$ $e^+e^- \rightarrow (h)(h)X$
PRD 88 (2013) 032011 (Babar)	PRD 92 (2015) 111101 (Babar K) PRL 116 (2016) 042001 (BESIII)	and scale dependence
Transverse momentum dependent FFs: $e^+e^- \rightarrow (h)X$ $D_{1,q}^h(z, k_T, Q^2)$	Transverse momentum dependent asymmetries $e^+e^- \rightarrow (h)(h)X,$ $\cos(\phi_1 + \phi_2), Q_t$ $H_{1,q}^{\perp h}(z, k_T, Q^2)$	
	PRD 90 (2014) 052003 (Babar)	

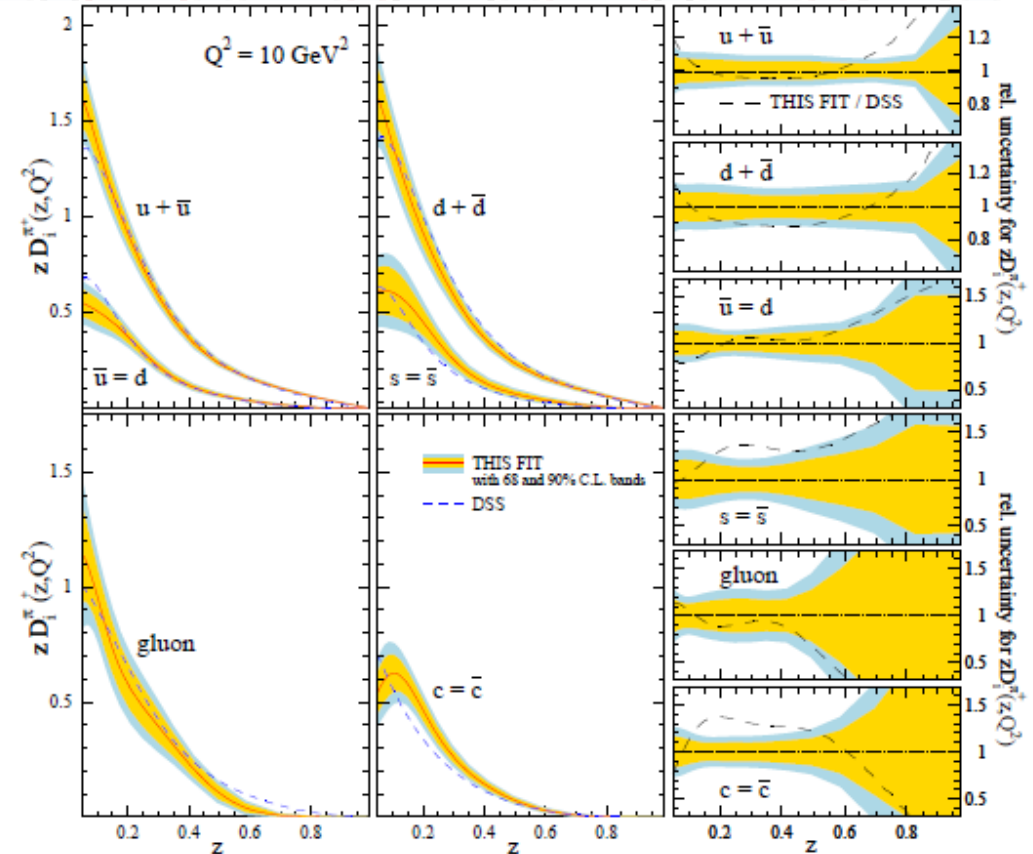
Dihadron measurements

Unpolarized ingredients	Polarized ingredients	Flavor sensitivity
Dihadron cross sections $e^+e^- \rightarrow (hh)X$ $D_{1,q}^{h_1 h_2}(z, m, Q^2)$	Azimuthal asymmetries: $e^+e^- \rightarrow (hh)(hh)X,$ $\cos(\phi_1 + \phi_2),$ $H_{1,q}^{h_1, h_2, \triangleleft}(z, Q^2, M_h)$	Unpol SIDIS, pp: $\frac{d^2\sigma}{dzdm}$
5/30/2024	Ralf Seidl: Fragmentation for EIC	

Pion fragmentation

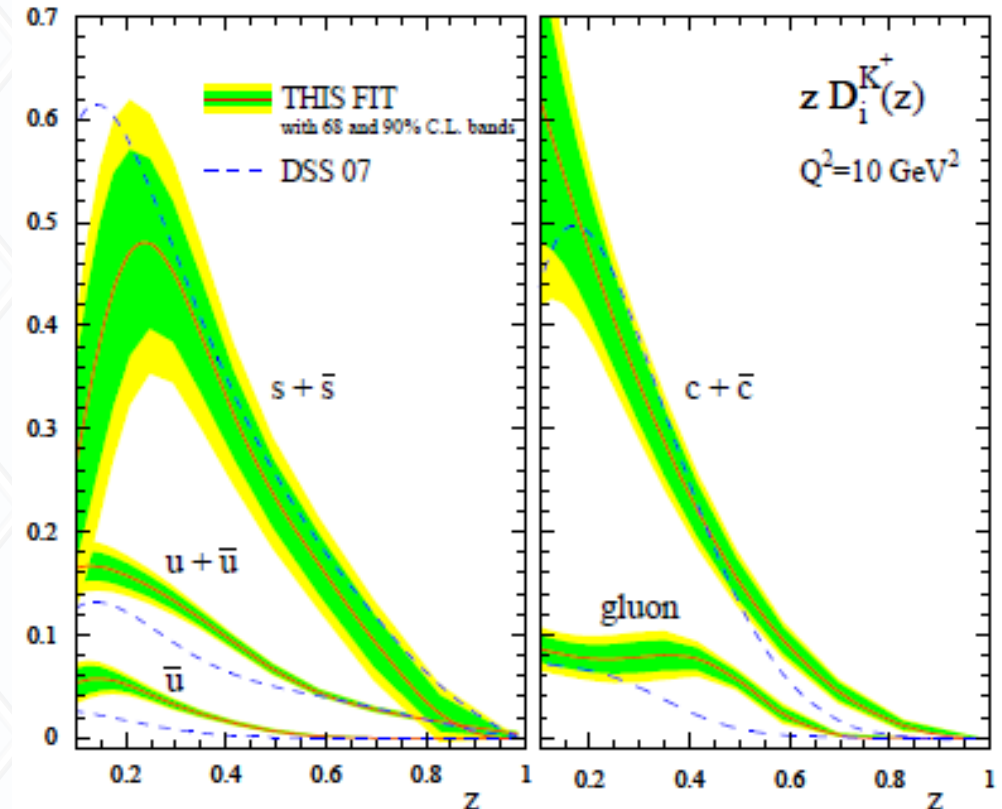
DSS15: [deFlorian et.al., Phys.Rev. D91 \(2015\) 014035](#)

- Light quarks symmetric
- Dominated by favored fragmentation especially at high z
- Gluon substantial but falling off faster than quarks



Kaon fragmentation

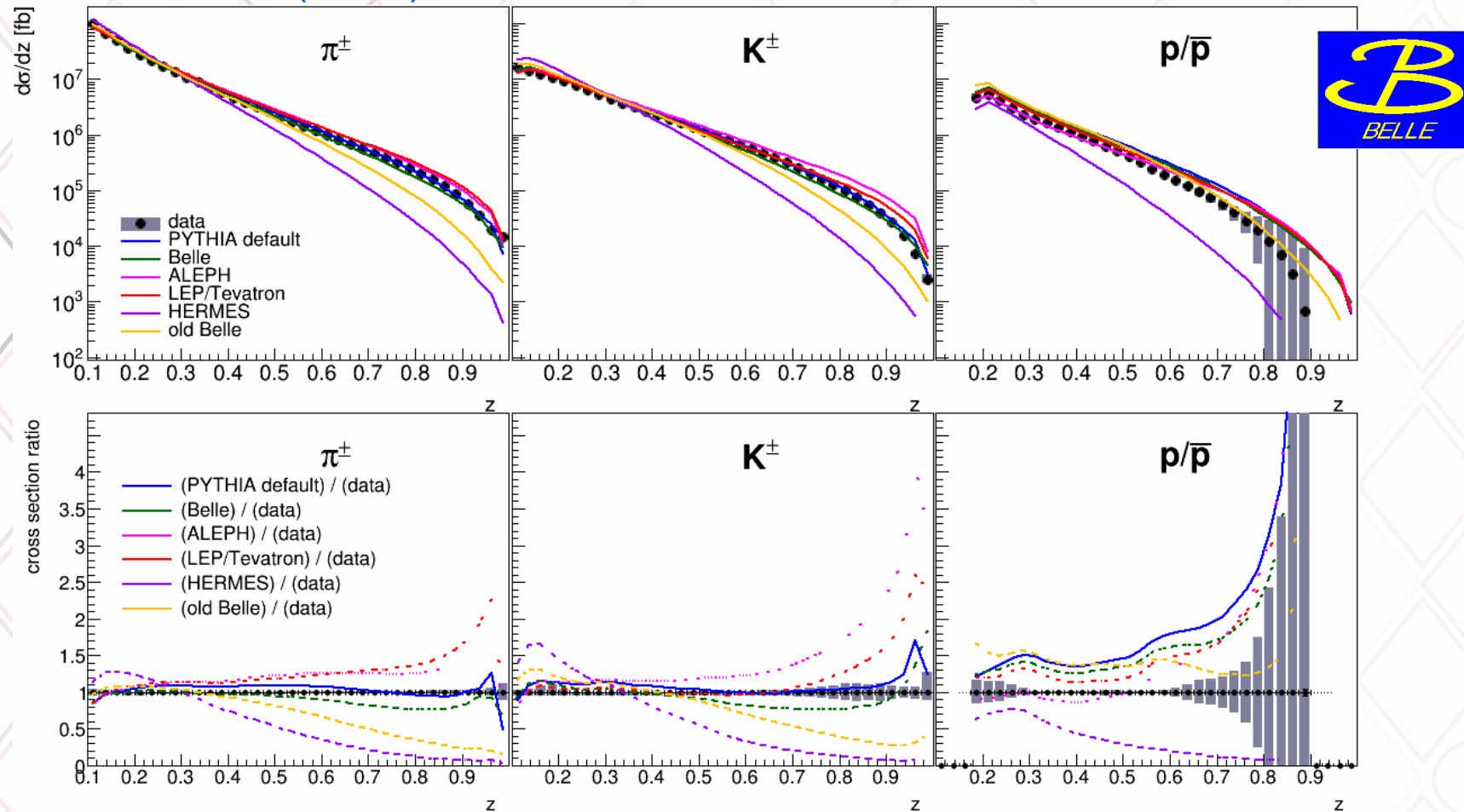
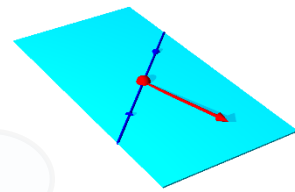
- Strange quarks are dominating kaon fragmentation
- Also dominated by favored u quark fragmentation at high-z
- At lower z penalty for producing $s\bar{s}$ pair in fragmentation ($u+\bar{u} < s+\bar{s}$)
- Charm fragmentation comparable (what about weak decays?)



[DEHSS *Phys.Rev.D* 95 \(2017\) 9, 094019](#)

Unpolarized single hadrons

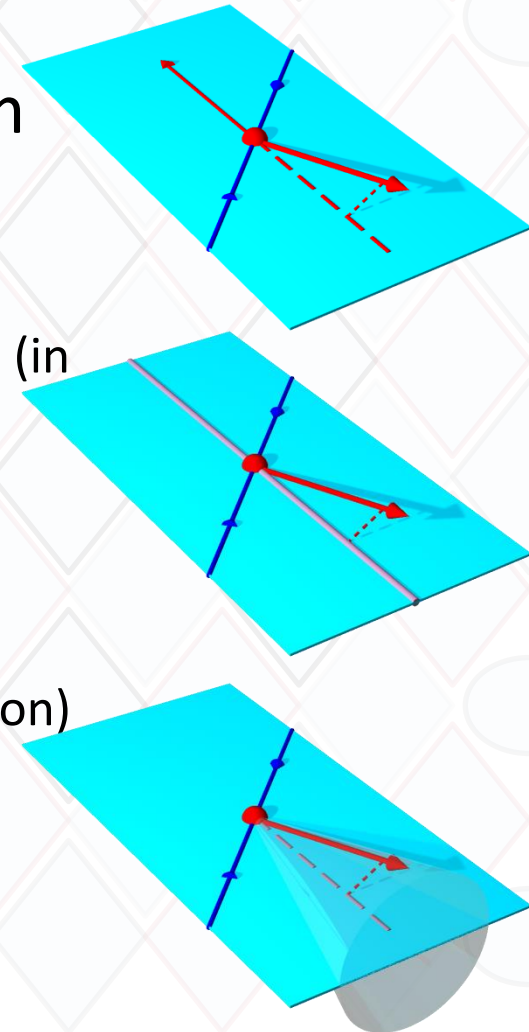
PRD 101 (2020) 092004



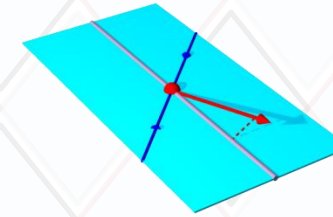
- Update with better ISR correction
- Correlated and uncorrelated uncertainties separated → improve global unpolarized FF fits

K_T Dependence of FFs in $e+e^-$

- Gain also sensitivity into transverse momentum generated in fragmentation
- Two ways to obtain transverse momentum dependence
 - Traditional 2-hadron FF
 - use transverse momentum between two hadrons (in opposite hemispheres)
 - Usual convolution of two transverse momenta
 - Single-hadron FF wrt to **Thrust** or jet axis
 - No convolution
 - Need correction for $q\bar{q}$ axis (similar to a Jet function)

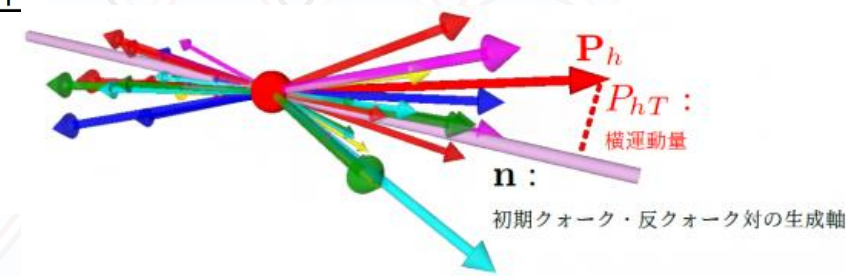
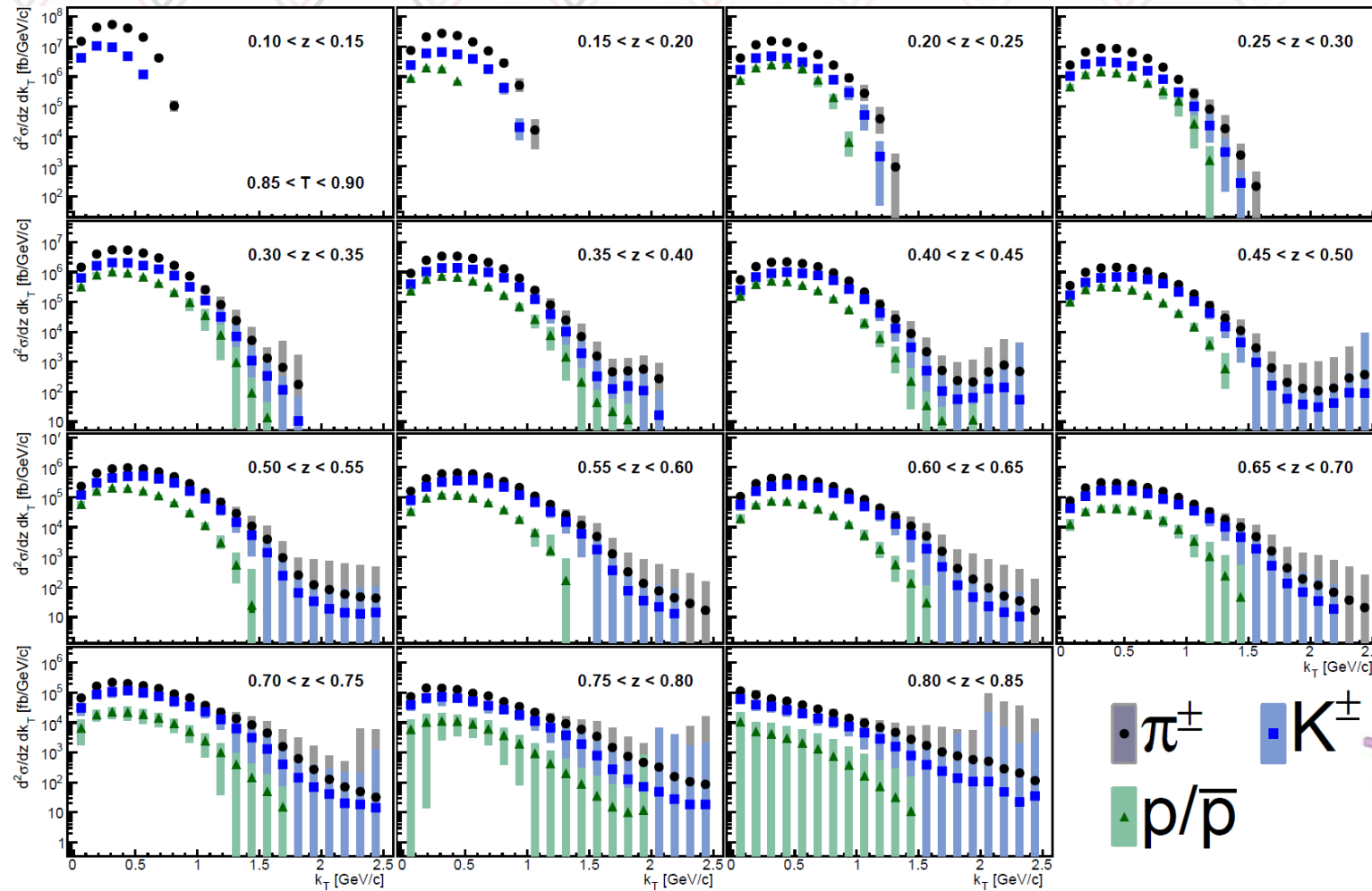


Transverse momentum dependent cross sections for pions, kaons and protons



Important baseline for most transverse momentum/spin dependent measurements at RHIC and EIC

RIKEN Press release:
https://www.riken.jp/press/2019/20190615_1/



$$\frac{d^2\sigma}{dz dP_{hT}}$$



RS. et. al. [PRD99 \(2019\) 112006](#)

Ralf Seidl: Fragmentation for EIC

5/30/2024

Gaussian widths comparison to MC

first direct (no convolutions) measurement of z dependence of Gaussian widths

MSTP(21):

0.28

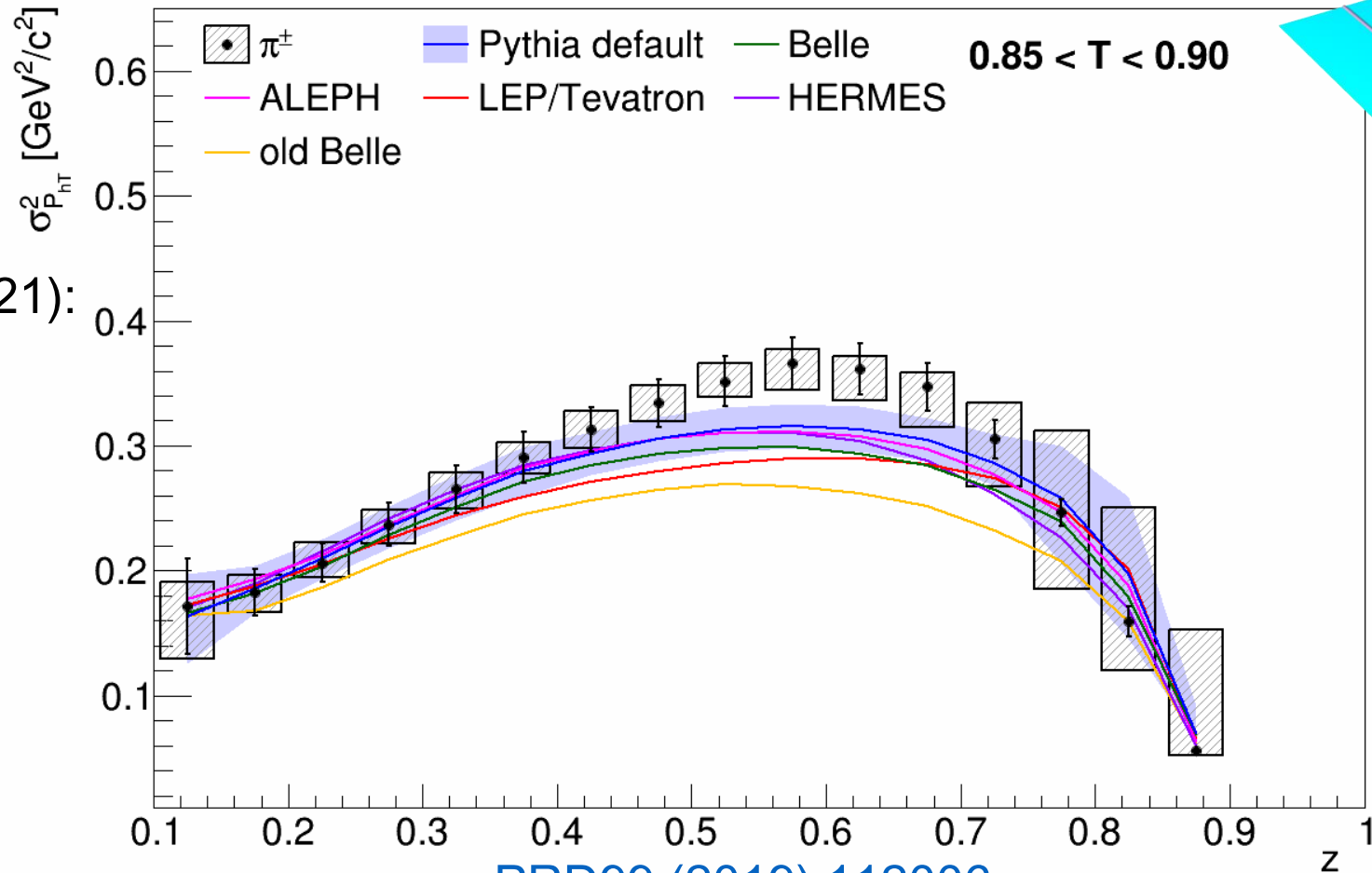
0.325

0.36

0.36

0.37

0.40

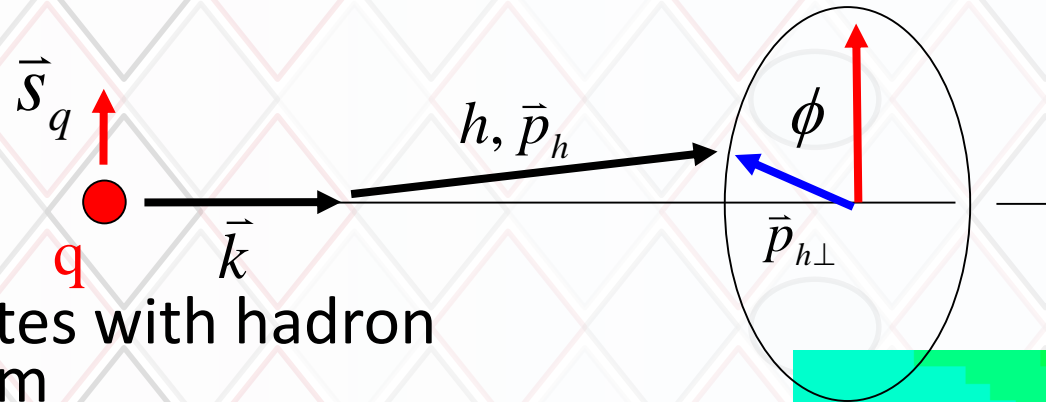


[PRD99 \(2019\) 112006](#)

Collins fragmentation function

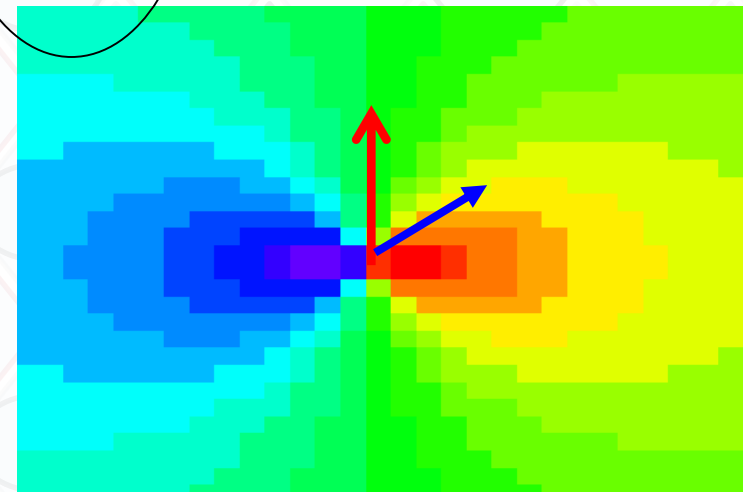
J. Collins, Nucl. Phys. B396, (1993) 161

$$D_{q\uparrow}^h(z, P_{h\perp}) = D_{1,q}^h(z, P_{h\perp}^2) + H_{1,q}^{\perp h}(z, P_{h\perp}^2) \frac{(\hat{\mathbf{k}} \times \mathbf{P}_{h\perp}) \cdot \mathbf{S}_q}{zM_h}$$



- Spin of quark correlates with hadron transverse momentum
- ➔ translates into azimuthal anisotropy of final state hadrons

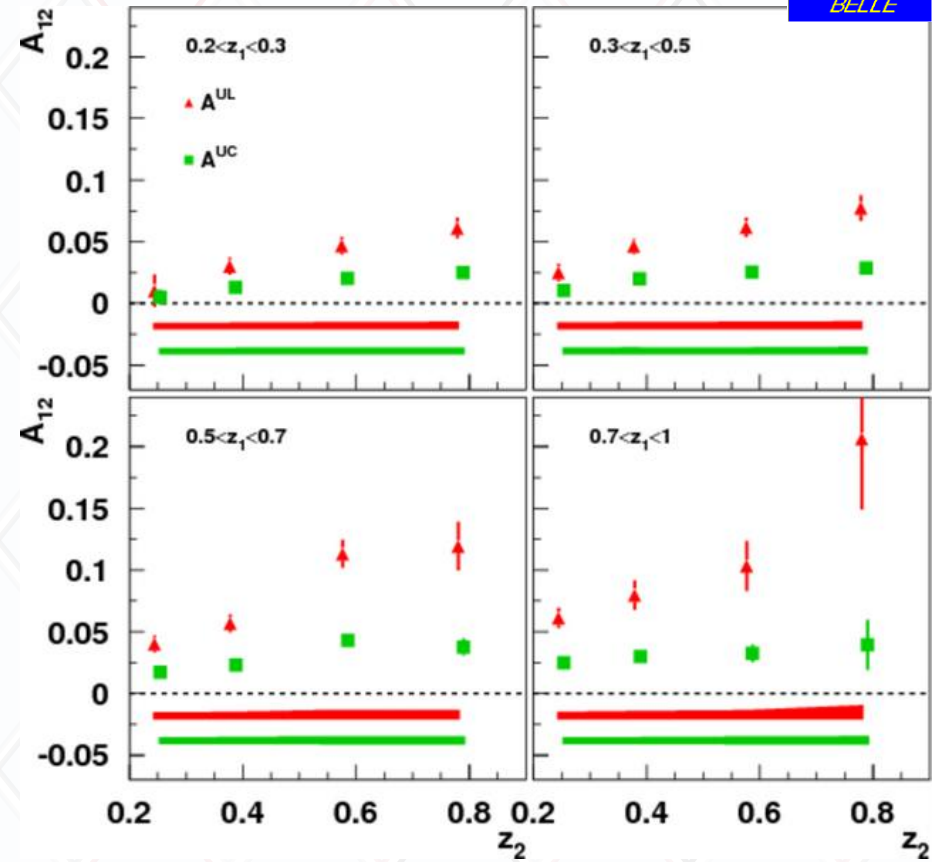
Needed at the EIC to access Transversity and Boer-Mulders (quark spin-orbit) function



Belle Collins asymmetries



- **Red points** : $\cos(\phi_1 + \phi_2)$ moment of **Unlike** sign pion pairs over **like** sign pion pair ratio : A^{UL}
- **Green points** : $\cos(\phi_1 + \phi_2)$ moment of **Unlike** sign pion pairs over **any charged** pion pair ratio : A^{UC}
- Collins fragmentation is large effect
- Consistent with SIDIS indication of sign change between favored and disfavored Collins FF

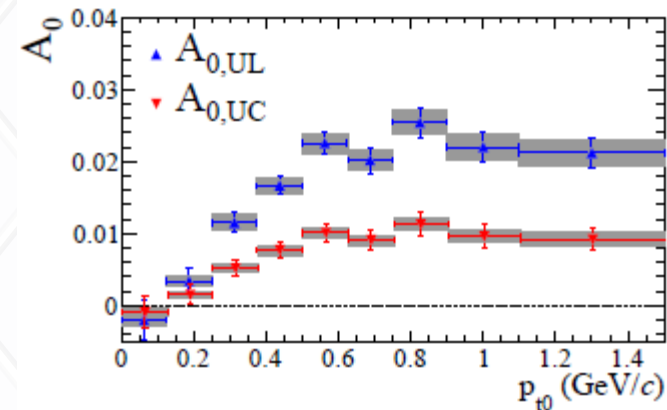
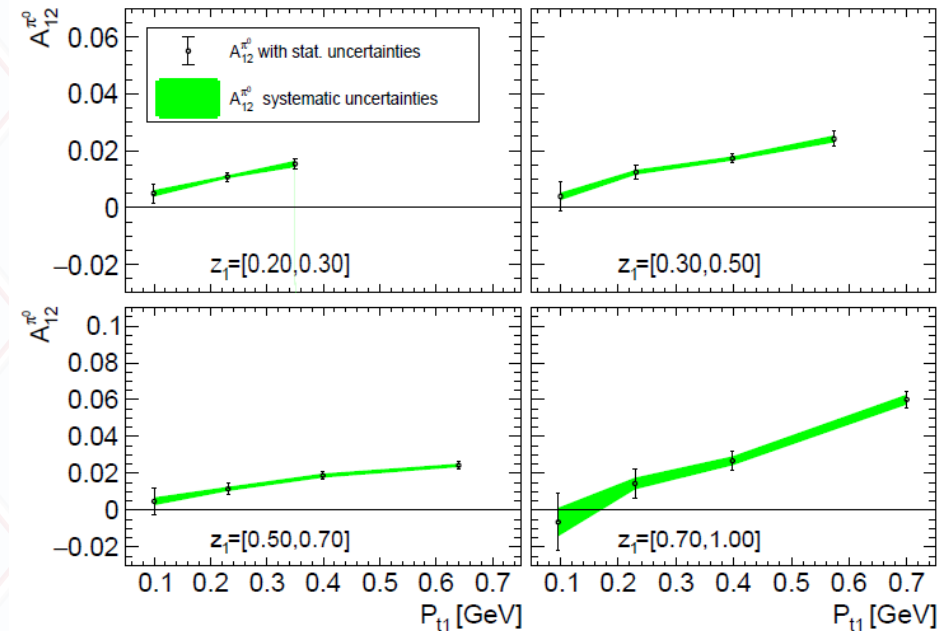


RS et al (Belle), PRL96: 232002
PRD 78:032011, Erratum D86:039905

Transverse momentum

- Add transverse momentum to Collins asymmetries' z dependence
- Currently only 1 or 2-dimensional extractions available ($q_t, z_1 \times z_2, p_{t1} \times p_{t2}, z_1 \times p_{t1}$)
- Increasing asymmetries with both z and p_t , but p_t reach limited
- Multidimensional extractions needed

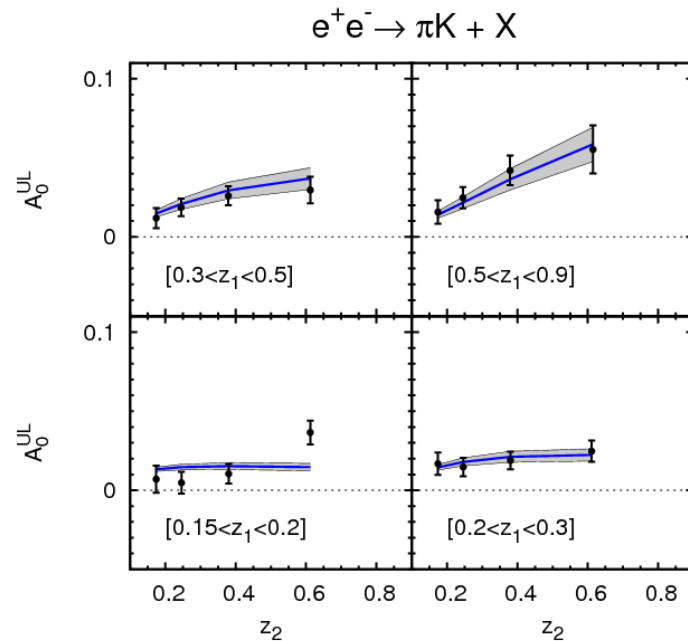
[PRD100 \(2019\) 92008](#)



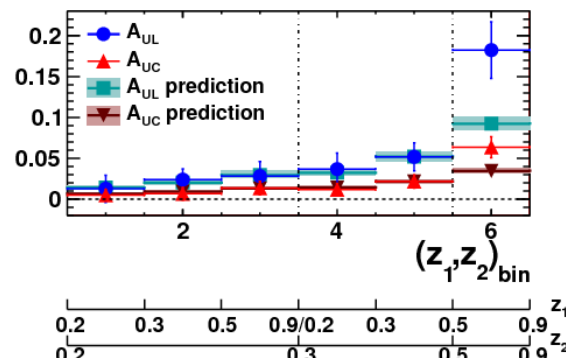
Quark transversity via Collins: Kaons

BABAR: [PRD 92 \(2015\) 111101](#)

Anselmino et al: [PRD 93 \(2016\) 034025](#)



BESIII: [PRL 116 \(2016\) 042001](#)

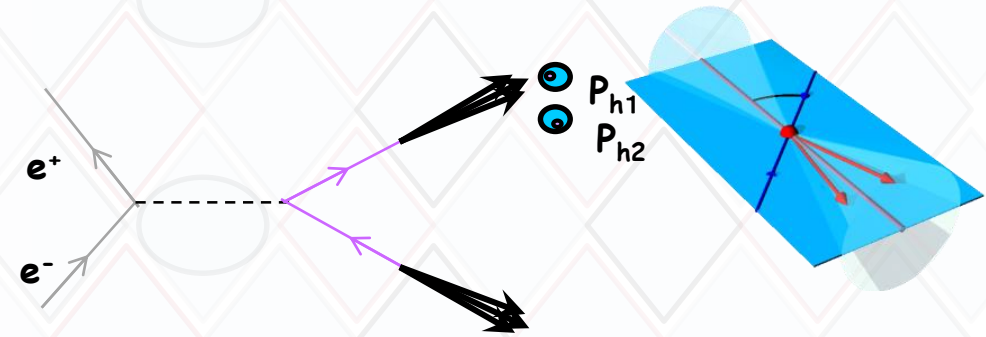


- Addition of kaon Collins fragmentation strongly needed for flavor decomposition of quark transversity
- Large amount of potentially participating FFs well described by light and “heavy” favored and disfavored FFs
- Allows inclusion of HERMES and COMPASS kaon asymmetries (+eventually EIC) in fits
- Also: pion Collins at lower scale (BESIII) consistent with TMD evolution

Di-hadron fragmentation functions

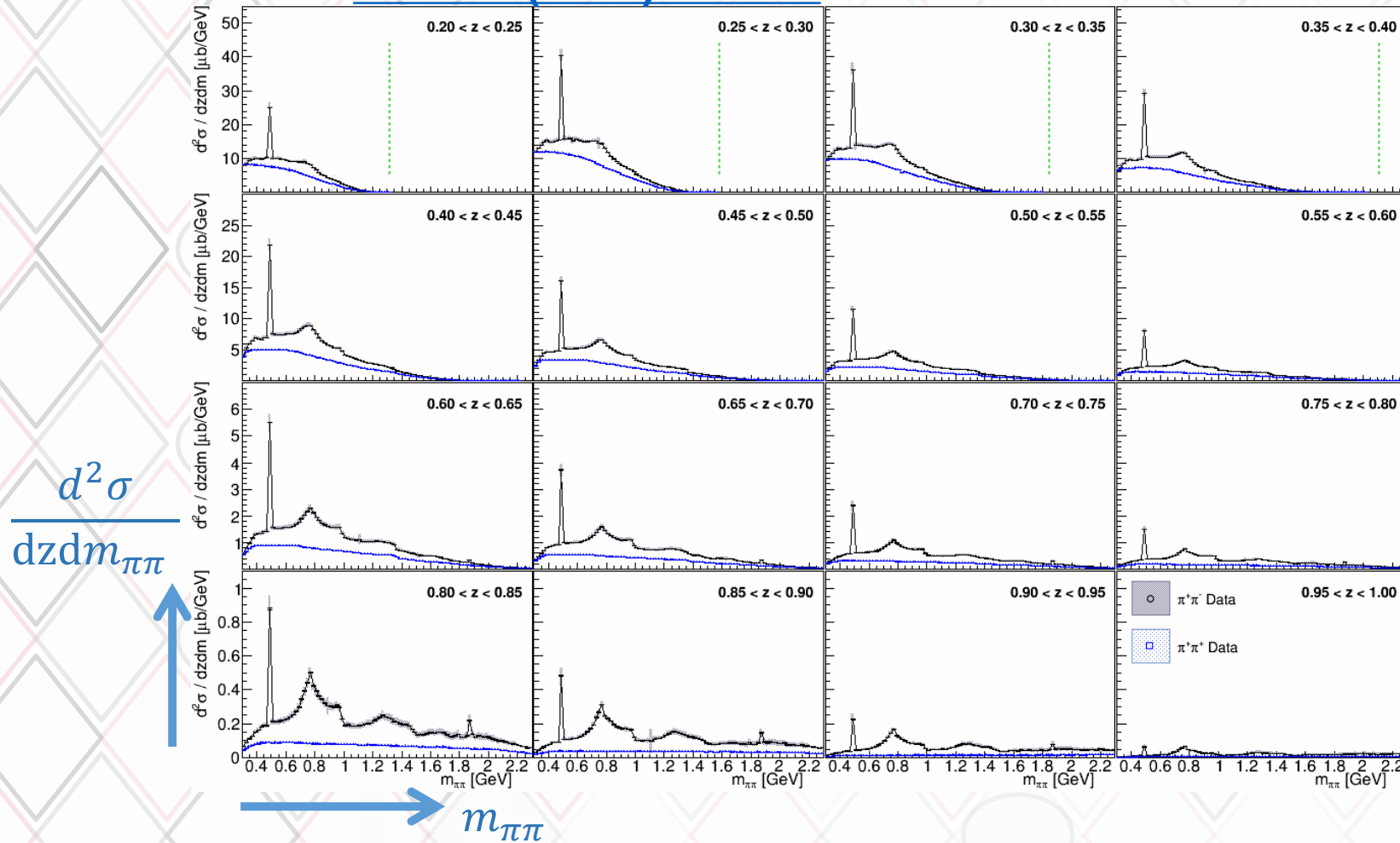
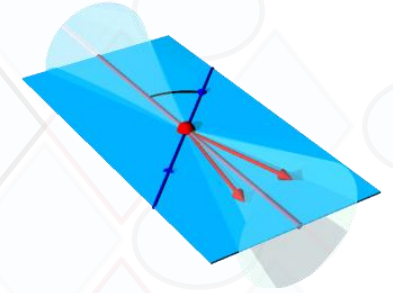
$$D_{1,q}^{h_1 h_2}(z, m, Q^2)$$

and transverse spin dependent interference fragmentation function



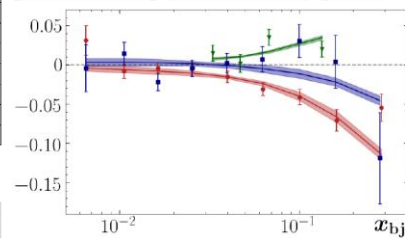
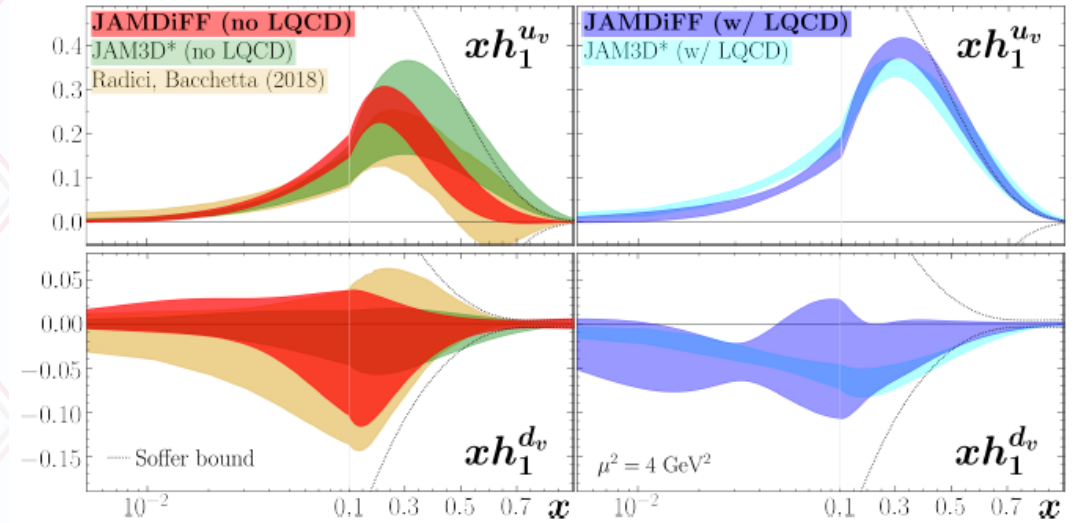
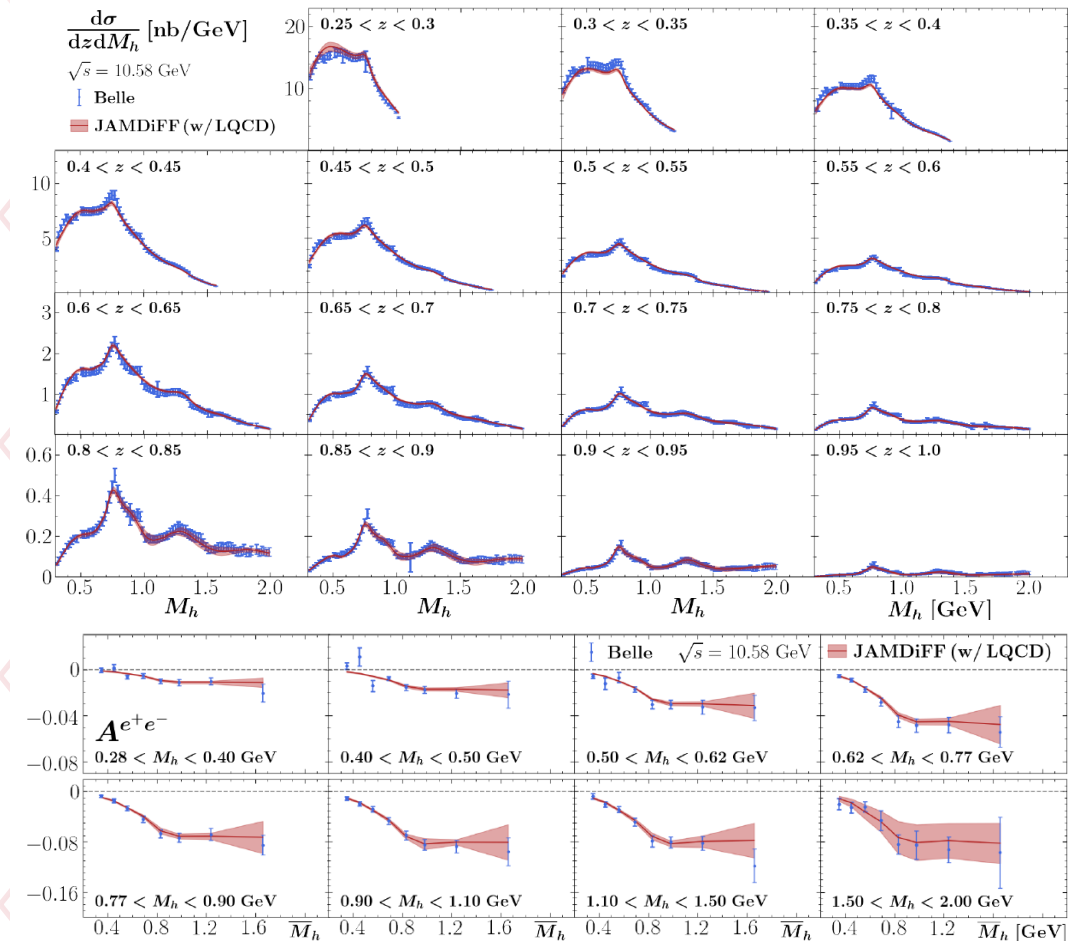
Di-hadron FF mass dependence (same hemisphere)

Belle: RS et.al. [PRD96 \(2017\) 032005](#)



- Important input for IFF based transversity global analysis
- Individual resonances, etc quite visible; interesting for FF in itself (\rightarrow soon)

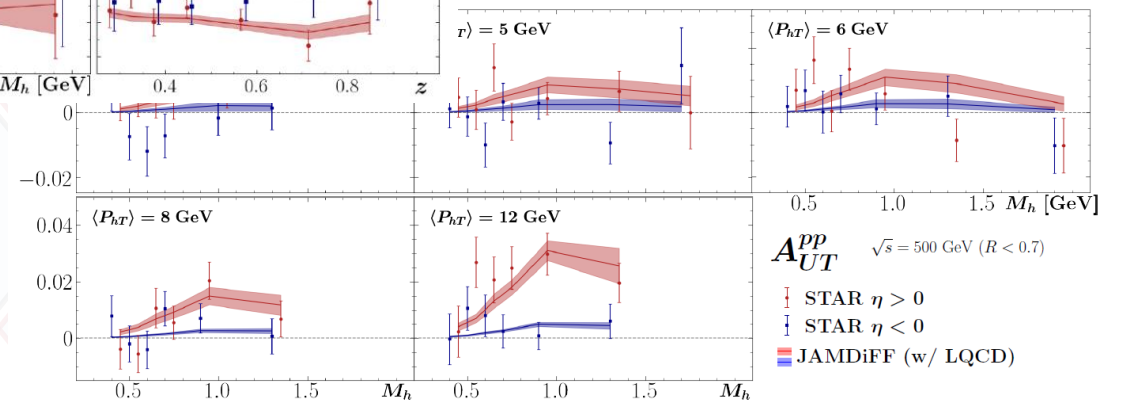
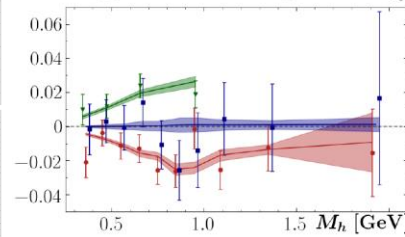
Global fits of Dihadron FFs



Cocuzza et al.

<https://arxiv.org/abs/2306.12998>

Also Radici et al. *PRL* 120 (2018) 19, 192001

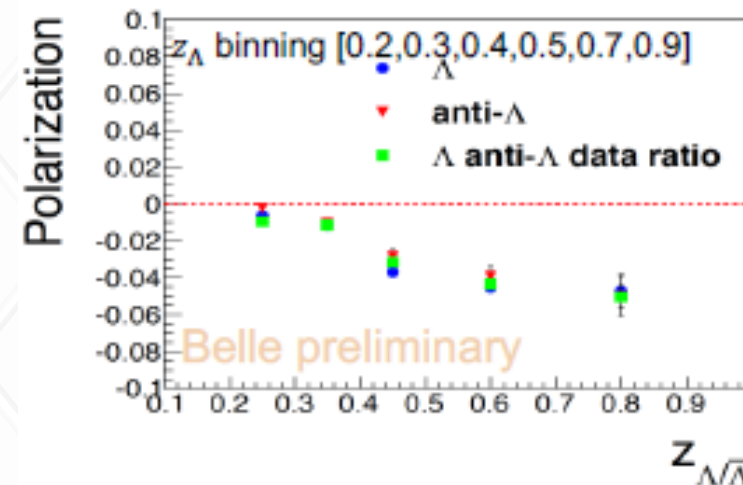
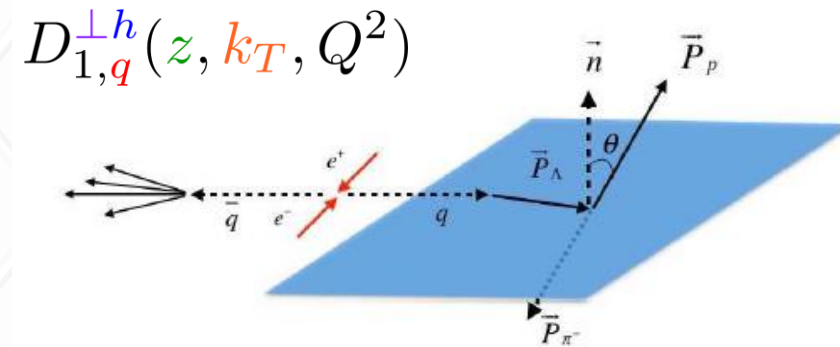


- Global fits taking SIDIS data, RHIC data, Belle data (polarized and unpolarized) into account

Single Λ polarization measurements

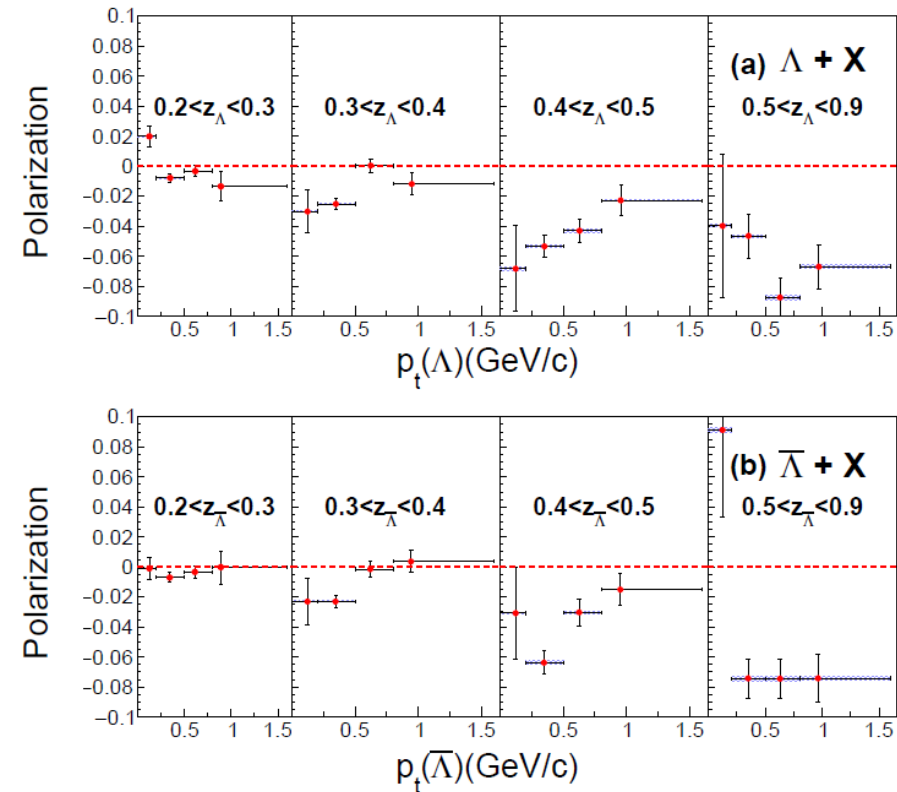
- Related to open question about Λ polarization in hadron collisions from 40 years ago!
- Fragmentation counterpart to the Sivers Function:
 - unpolarized parton fragments into transversely polarized baryon with transverse momentum wrt to parton direction
- Reconstruct Λ , its transverse momentum and polarization

YingHui Guan (Indiana/KEK):
[PRL 122 \(2019\), 042001](#)



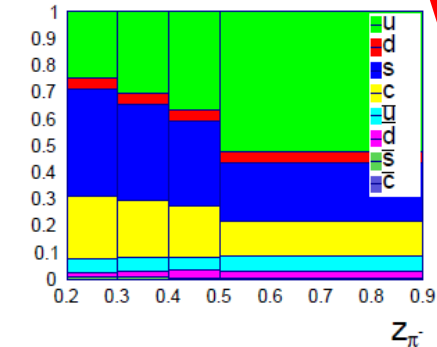
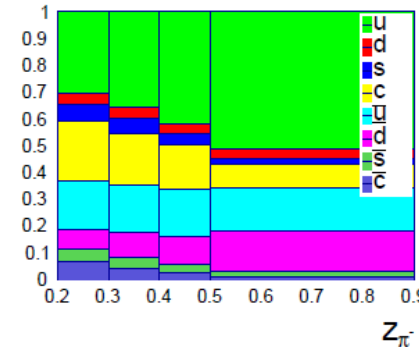
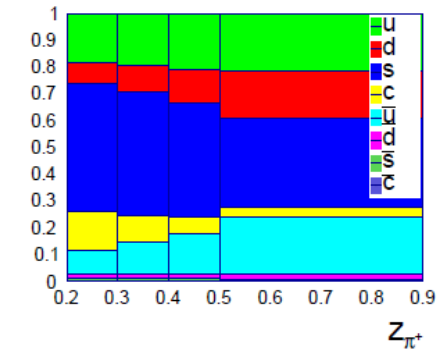
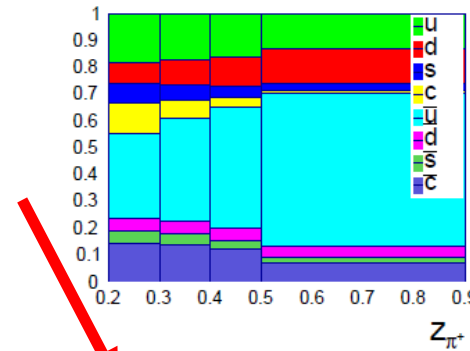
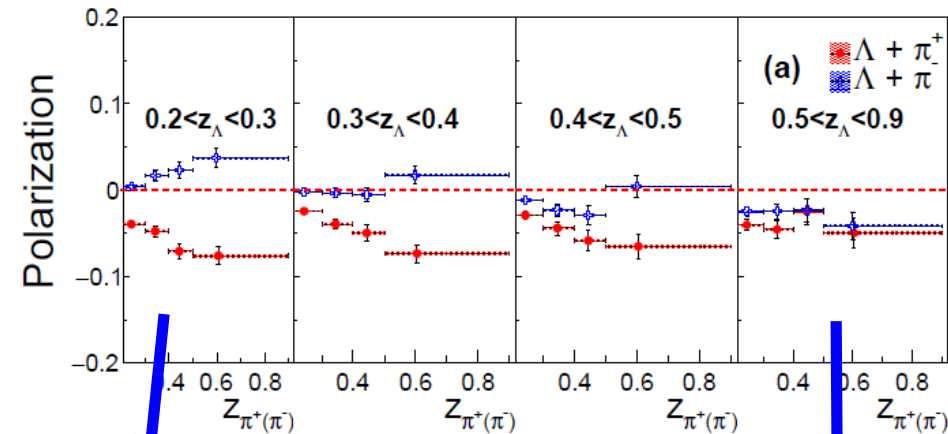
Transverse momentum dependence

- Different behavior for low and high- z :
- At low z small
- At intermediate z falling Polarization with P_t
- At high z increasing polarization with P_t



Opposite hemisphere pion correlation

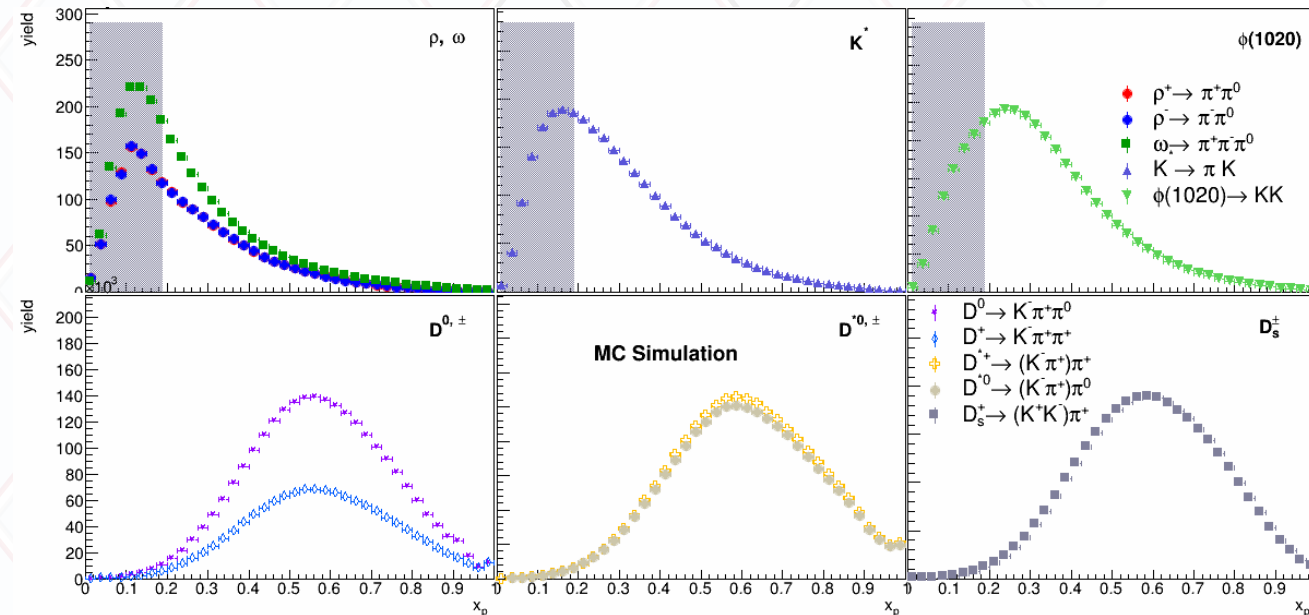
- Interesting z_π and z_Λ dependence :
- At low z_Λ light quark fragmentation dominant, some charm in $\pi^- \rightarrow$ different signs
- At high z_Λ strange + charm fragmentation more relevant \rightarrow same signs
- Several fits to data with slightly different results



Ongoing: Decaying particle FFs

- Study the explicit differential cross sections for VMs, D mesons as a function of x_p
- Mostly mass distributions and fits well-behaved, except for ρ – ω (interference) and more exotic resonances
- Also of interest for ultra high-energetic cosmic ray air shower research (muon problem)

- Example from MC at Belle energies (for 4π acceptance):



Important resource for EIC, RHIC and HI physics

Summary

- Fragmentation functions are crucial to access the goals of the EIC in semi-inclusive DIS:
 - Unpolarized FFs are needed for unpolarized (n)PDFs and (anti)quark spin contributions
 - Polarized FFs are needed for Transversity and tensor charge
 - Transverse momentum dependent FFs for
- Many relevant FF measurements obtained from B factories, more to come
- At the EIC the spin structure and the 3 Dimensional momentum structure of the nucleon will be accessed and greatly improved compared to the current knowledge